Project_Code_1e.m

By Joshua Norlin This project code calculates the characteristic exponents of the rotor system without reversed flow for values B=1 and p=1.2, determines the stability of the system, and plots the results. Stable1 and Stable2 contain a true/false analysis for each characteristic exponent's stability, and Nu contains the characteristic exponent pairs. For gamma=0:16, values 1:17 correspond with mu=0, values 18:34 correspond with mu=1, and values 35:51 correspond with mu=2.

```
t = 0:pi/8:2*pi;
conditions1 = [1 0];
conditions2 = [0 1];
Q = []; % Matrix of transition matricies; Values 1:34 are for mu=0,
 35:69
% are for mu=1, 70:102 are for mu=2.
Lambda = []; % Eigenvalues of transition matricies
Nu = []; % Natural logarithms of transition matricies
Stable1 = []; % Values of stability for Nu, 1=stable, 0=unstable
Stable2 = []; % Values of stability for Nu, 1=stable, 0=unstable
% Values 1:17 are for mu=0, gamma=0:16, 18:34 are for mu=1, and 35:51
 are
% for mu=2.
for mu = 0:2
    for gamma = 0:16
        [t,beta2] =
 ode45(@(t,beta)rhs(t,beta,mu,gamma),t,conditions2);
        [t,beta1] =
 ode45(@(t,beta)rhs(t,beta,mu,gamma),t,conditions1);
        Beta1 = beta1(:,1);
        Beta2 = beta2(:,1);
        dBeta1dt = beta1(:,2);
        dBeta2dt = beta2(:,2);
        period1a = Beta1(length(t));
        period1b = dBeta1dt(length(t));
        period2a = Beta2(length(t));
        period2b = dBeta2dt(length(t));
        q = [period1a period2a; period1b period2b];
        lambda = eig(q);
        nu = (1/(2*pi))*log(lambda);
       if real(nu(1)) <= 0
            stable1 = 1;
        elseif real(nu(1)) > 0
            stable1 = 0;
        end
        Stable1 = [Stable1 stable1];
        if real(nu(2)) <= 0
            stable2 = 1;
        elseif real(nu(2)) > 0
            stable2 = 0;
        end
        Stable2 = [Stable2 stable2];
        Q = [Q q];
        Lambda = [Lambda lambda];
```

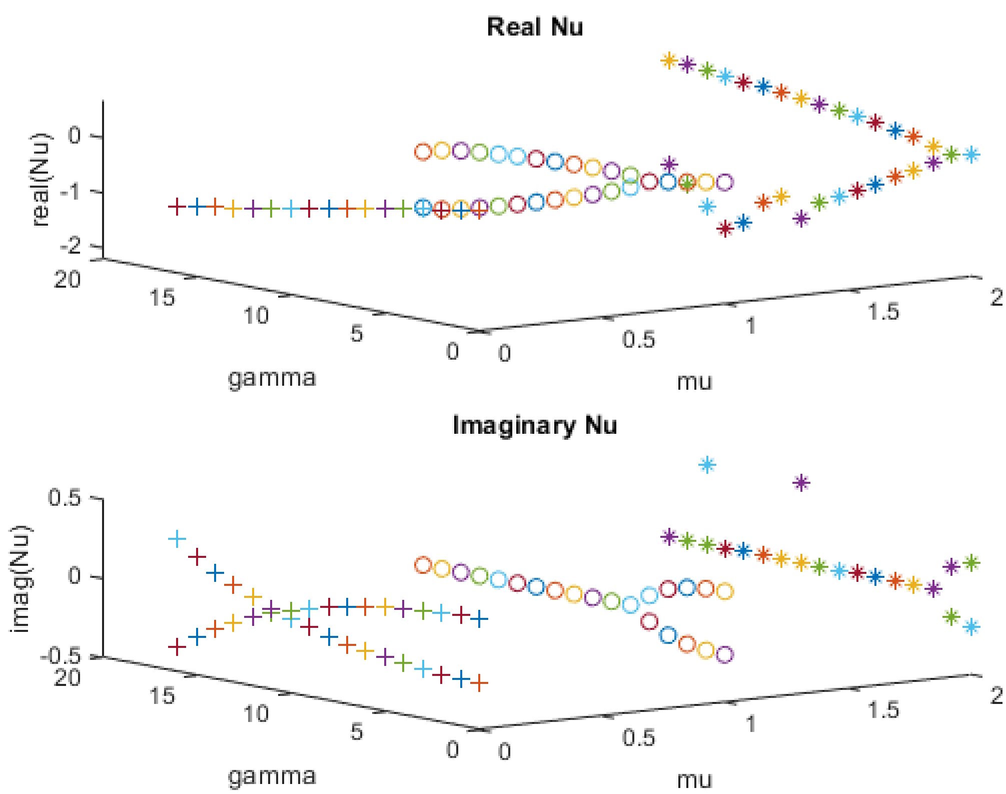
```
        Nu = [Nu nu];
    end
end
figure
hold on
mu = 0:2;
gamma = 0:16;
subplot(2,1,1)
for i = 1:length(gamma)
    plot3(mu(1),gamma(i),real(Nu(:,i)),'+')
    hold on
    plot3(mu(2),gamma(i),real(Nu(:,17+i)),'o')
    hold on
    plot3(mu(3),gamma(i),real(Nu(:,34+i)),'*')
    hold on
end
title('Real Nu')
xlabel('mu')
ylabel('gamma')
zlabel('real(Nu)')
subplot(2,1,2)
for i = 1:length(gamma)
     plot3(mu(1),gamma(i),imag(Nu(:,i)),'+')
    hold on
    plot3(mu(2),gamma(i),imag(Nu(:,17+i)),'o')
    hold on
    plot3(mu(3),gamma(i),imag(Nu(:,34+i)),'*')
    hold on
end
title('Imaginary Nu')
xlabel('mu')
ylabel('gamma')
zlabel('imag(Nu)')
Nu
Stable1
Stable2


function dbetadt = rhs(t,beta,mu,gamma)
B = 1;
p = 1.2;
K1 = gamma.*((B.^3).*mu.*cos(t)/6 + (B.^2).*(mu.^2).*sin(2.*t)/8);
K = K1;
C1 = gamma.*((B.^4)/8 + (B.^3).*mu.*sin(t)/6);
C = C1;
dbetadt_1 = beta(2);
dbetadt_2 = -(p.^2 + K).*beta(1) - C.*beta(2);
dbetadt = [dbetadt_1; dbetadt_2];
end
```

```
Nu =

  Columns 1 through 4
```

```
 -0.0000 + 0.2001i  -0.0626 + 0.1984i  -0.1251 + 0.1935i  -0.1876 +
0.1853i
 -0.0000 - 0.2001i  -0.0626 - 0.1984i  -0.1251 - 0.1935i  -0.1876 -
0.1853i

 Columns 5 through 8

 -0.2501 + 0.1737i  -0.3126 + 0.1585i  -0.3751 + 0.1398i  -0.4375 +
0.1173i
 -0.2501 - 0.1737i  -0.3126 - 0.1585i  -0.3751 - 0.1398i  -0.4375 -
0.1173i

 Columns 9 through 12

 -0.5000 + 0.0907i  -0.5624 + 0.0599i  -0.6249 + 0.0243i  -0.6874 +
0.0165i
 -0.5000 - 0.0907i  -0.5624 - 0.0599i  -0.6249 - 0.0243i  -0.6874 -
0.0165i

 Columns 13 through 16

 -0.7499 + 0.0632i  -0.8124 + 0.1169i  -0.8749 + 0.1787i  -0.9375 +
0.2508i
 -0.7499 - 0.0632i  -0.8124 - 0.1169i  -0.8749 - 0.1787i  -0.9375 -
0.2508i

 Columns 17 through 20

 -1.0001 + 0.3365i  -0.0000 + 0.2001i  -0.0625 + 0.1948i  -0.1250 +
0.1779i
 -1.0001 - 0.3365i  -0.0000 - 0.2001i  -0.0625 - 0.1948i  -0.1250 -
0.1779i

 Columns 21 through 24

 -0.1875 + 0.1457i  -0.2500 + 0.0820i  -0.2040 + 0.0000i  -0.1903 +
0.0000i
 -0.1875 - 0.1457i  -0.2500 - 0.0820i  -0.4211 + 0.0000i  -0.5599 +
0.0000i

 Columns 25 through 28

 -0.1924 + 0.0000i  -0.2014 + 0.0000i  -0.2147 + 0.0000i  -0.2317 +
0.0000i
 -0.6826 + 0.0000i  -0.7985 + 0.0000i  -0.9100 + 0.0000i  -1.0180 +
0.0000i

 Columns 29 through 32

 -0.2525 + 0.0000i  -1.2223 + 0.0000i  -1.3161 + 0.0000i  -1.4009 +
0.0000i
 -1.1224 + 0.0000i  -0.2779 + 0.0000i  -0.3094 + 0.0000i  -0.3501 +
0.0000i
```

```
  Columns 33 through 36

  -1.4770 + 0.0000i  -1.5112 + 0.0000i  -0.0000 + 0.2001i  -0.0625 +
 0.1577i
  -0.4066 + 0.0000i  -0.4979 + 0.0000i  -0.0000 - 0.2001i  -0.0625 -
 0.1577i

  Columns 37 through 40

   0.0141 + 0.0000i   0.1124 + 0.0000i   0.1797 + 0.0000i   0.2368 +
 0.0000i
  -0.2641 + 0.0000i  -0.4877 + 0.0000i  -0.6801 + 0.0000i  -0.8868 +
 0.0000i

  Columns 41 through 44

   0.2881 + 0.0000i   0.3356 + 0.0000i   0.3801 + 0.0000i   0.4221 +
 0.0000i
  -1.0408 + 0.0000i  -1.2142 + 0.0000i  -1.4137 + 0.0000i  -1.7417 +
 0.5000i

  Columns 45 through 48

   0.4622 + 0.0000i   0.5004 + 0.0000i   0.5369 + 0.0000i   0.5717 +
 0.0000i
  -1.4133 + 0.0000i  -1.5807 + 0.0000i  -2.0235 + 0.0000i  -2.2092 +
 0.0000i

  Columns 49 through 51

   0.6048 + 0.0000i   0.6359 + 0.0000i   0.6649 + 0.0000i
  -1.8727 + 0.5000i  -1.5202 + 0.0000i  -1.2521 + 0.0000i


Stable1 =

  Columns 1 through 13

     1     1     1     1     1     1     1     1     1     1     1
 1     1

  Columns 14 through 26

     1     1     1     1     1     1     1     1     1     1     1
 1     1

  Columns 27 through 39

     1     1     1     1     1     1     1     1     1     1     0
 0     0

  Columns 40 through 51
```

```
     0     0     0     0     0     0     0     0     0     0     0
  0


Stable2 =

  Columns 1 through 13

     1     1     1     1     1     1     1     1     1     1     1
 1     1

  Columns 14 through 26

     1     1     1     1     1     1     1     1     1     1     1
 1     1

  Columns 27 through 39

     1     1     1     1     1     1     1     1     1     1     1
 1     1

  Columns 40 through 51

     1     1     1     1     1     1     1     1     1     1     1
  1
```



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