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# Project\_Code\_1b.m

By Joshua Norlin This project code calculates the characteristic exponents of the rotor system without reversed flow for values  $B=0.98$  and  $p=1.2$ , determines the stability of the system, and plots the results. Stable1 and Stable2 contain a true/false analysis for each characteristic exponent's stability, and Nu contains the characteristic exponent pairs. For  $\gamma=0:16$ , values 1:17 correspond with  $\mu=0$ , values 18:34 correspond with  $\mu=1$ , and values 35:51 correspond with  $\mu=2$ .

```
t = 0:pi/8:2*pi;
conditions1 = [1 0];
conditions2 = [0 1];
Q = []; % Matrix of transition matrices; Values 1:34 are for mu=0,
35:69
% are for mu=1, 70:102 are for mu=2.
Lambda = []; % Eigenvalues of transition matrices
Nu = []; % Natural logarithms of transition matrices
Stable1 = []; % Values of stability for Nu, 1=stable, 0=unstable
Stable2 = []; % Values of stability for Nu, 1=stable, 0=unstable
% Values 1:17 are for mu=0, gamma=0:16, 18:34 are for mu=1, and 35:51
are
% for mu=2.
for mu = 0:2
    for gamma = 0:16
        [t,beta2] =
ode45(@(t,beta)rhs(t,beta,mu,gamma),t,conditions2);
        [t,beta1] =
ode45(@(t,beta)rhs(t,beta,mu,gamma),t,conditions1);
        Beta1 = beta1(:,1);
        Beta2 = beta2(:,1);
        dBeta1dt = beta1(:,2);
        dBeta2dt = beta2(:,2);
        period1a = Beta1(length(t));
        period1b = dBeta1dt(length(t));
        period2a = Beta2(length(t));
        period2b = dBeta2dt(length(t));
        q = [period1a period2a; period1b period2b];
        lambda = eig(q);
        nu = (1/(2*pi))*log(lambda);
        if real(nu(1)) <= 0
            stable1 = 1;
        elseif real(nu(1)) > 0
            stable1 = 0;
        end
        Stable1 = [Stable1 stable1];
        if real(nu(2)) <= 0
            stable2 = 1;
        elseif real(nu(2)) > 0
            stable2 = 0;
        end
        Stable2 = [Stable2 stable2];
        Q = [Q q];
        Lambda = [Lambda lambda];
    end
end
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        Nu = [Nu nu];
    end
end
figure
hold on
mu = 0:2;
gamma = 0:16;
subplot(2,1,1)
for i = 1:length(gamma)
    plot3(mu(1),gamma(i),real(Nu(:,i)),'+')
    hold on
    plot3(mu(2),gamma(i),real(Nu(:,17+i)),'o')
    hold on
    plot3(mu(3),gamma(i),real(Nu(:,34+i)),'*')
    hold on
end
title('Real Nu')
xlabel('mu')
ylabel('gamma')
zlabel('real(Nu)')
subplot(2,1,2)
for i = 1:length(gamma)
    plot3(mu(1),gamma(i),imag(Nu(:,i)),'+')
    hold on
    plot3(mu(2),gamma(i),imag(Nu(:,17+i)),'o')
    hold on
    plot3(mu(3),gamma(i),imag(Nu(:,34+i)),'*')
    hold on
end
title('Imaginary Nu')
xlabel('mu')
ylabel('gamma')
zlabel('imag(Nu)')
Nu
Stable1
Stable2

function dbetadt = rhs(t,beta,mu,gamma)
B = 0.98;
p = 1.2;
K1 = gamma.*((B.^3).*mu.*cos(t)/6 + (B.^2).*(mu.^2).*sin(2.*t)/8);
K = K1;
C1 = gamma.*((B.^4)/8 + (B.^3).*mu.*sin(t)/6);
C = C1;
dbetadt_1 = beta(2);
dbetadt_2 = -(p.^2 + K).*beta(1) - C.*beta(2);
dbetadt = [dbetadt_1; dbetadt_2];
end

Nu =

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*Columns 1 through 4*

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$-0.0000 + 0.2001i \quad -0.0577 + 0.1987i \quad -0.1154 + 0.1945i \quad -0.1730 + 0.1875i$   
 $-0.0000 - 0.2001i \quad -0.0577 - 0.1987i \quad -0.1154 - 0.1945i \quad -0.1730 - 0.1875i$

Columns 5 through 8

$-0.2307 + 0.1776i \quad -0.2883 + 0.1648i \quad -0.3460 + 0.1490i \quad -0.4036 + 0.1300i$   
 $-0.2307 - 0.1776i \quad -0.2883 - 0.1648i \quad -0.3460 - 0.1490i \quad -0.4036 - 0.1300i$

Columns 9 through 12

$-0.4612 + 0.1077i \quad -0.5188 + 0.0819i \quad -0.5764 + 0.0523i \quad -0.6340 + 0.0187i$   
 $-0.4612 - 0.1077i \quad -0.5188 - 0.0819i \quad -0.5764 - 0.0523i \quad -0.6340 - 0.0187i$

Columns 13 through 16

$-0.6917 + 0.0195i \quad -0.7493 + 0.0628i \quad -0.8070 + 0.1119i \quad -0.8646 + 0.1679i$   
 $-0.6917 - 0.0195i \quad -0.7493 - 0.0628i \quad -0.8070 - 0.1119i \quad -0.8646 - 0.1679i$

Columns 17 through 20

$-0.9223 + 0.2322i \quad -0.0000 + 0.2001i \quad -0.0577 + 0.1954i \quad -0.1153 + 0.1805i$   
 $-0.9223 - 0.2322i \quad -0.0000 - 0.2001i \quad -0.0577 - 0.1954i \quad -0.1153 - 0.1805i$

Columns 21 through 24

$-0.1730 + 0.1527i \quad -0.2306 + 0.1020i \quad -0.2100 + 0.0000i \quad -0.1842 + 0.0000i$   
 $-0.1730 - 0.1527i \quad -0.2306 - 0.1020i \quad -0.3666 + 0.0000i \quad -0.5078 + 0.0000i$

Columns 25 through 28

$-0.1810 + 0.0000i \quad -0.1855 + 0.0000i \quad -0.1944 + 0.0000i \quad -0.2065 + 0.0000i$   
 $-0.6263 + 0.0000i \quad -0.7369 + 0.0000i \quad -0.8434 + 0.0000i \quad -0.9461 + 0.0000i$

Columns 29 through 32

$-0.2216 + 0.0000i \quad -0.2399 + 0.0000i \quad -1.2364 + 0.0000i \quad -1.3262 + 0.0000i$   
 $-1.0468 + 0.0000i \quad -1.1437 + 0.0000i \quad -0.2618 + 0.0000i \quad -0.2886 + 0.0000i$

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Columns 33 through 36

$-1.4069 + 0.0000i$   $-1.4788 + 0.0000i$   $-0.0000 + 0.2001i$   $-0.0577 + 0.1618i$   
 $-0.3222 + 0.0000i$   $-0.3666 + 0.0000i$   $-0.0000 - 0.2001i$   $-0.0577 - 0.1618i$

Columns 37 through 40

$0.0039 + 0.0000i$   $0.1077 + 0.0000i$   $0.1759 + 0.0000i$   $0.2333 + 0.0000i$   
 $-0.2345 + 0.0000i$   $-0.4543 + 0.0000i$   $-0.6355 + 0.0000i$   $-0.8077 + 0.0000i$

Columns 41 through 44

$0.2848 + 0.0000i$   $0.3323 + 0.0000i$   $0.3768 + 0.0000i$   $0.4190 + 0.0000i$   
 $-0.9658 + 0.0000i$   $-1.1542 + 0.0000i$   $-1.3379 + 0.0000i$   $-1.4329 + 0.5000i$

Columns 45 through 48

$0.4591 + 0.0000i$   $0.4977 + 0.0000i$   $0.5346 + 0.0000i$   $0.5702 + 0.0000i$   
 $-1.4274 + 0.5000i$   $-1.5125 + 0.0000i$   $-1.7819 + 0.0000i$   $-1.7936 + 0.5000i$

Columns 49 through 51

$0.6044 + 0.0000i$   $0.6372 + 0.0000i$   $0.6685 + 0.0000i$   
 $-1.6761 + 0.0000i$   $-2.0708 + 0.0000i$   $-1.3449 + 0.0000i$

Stable1 =

Columns 1 through 13

1 1 1 1 1 1 1 1 1 1 1  
1 1

Columns 14 through 26

1 1 1 1 1 1 1 1 1 1 1  
1 1

Columns 27 through 39

1 1 1 1 1 1 1 1 1 1 0  
0 0

Columns 40 through 51

0 0 0 0 0 0 0 0 0 0 0 0  
 0

Stable2 =

Columns 1 through 13

1 1 1 1 1 1 1 1 1 1 1 1  
 1 1

Columns 14 through 26

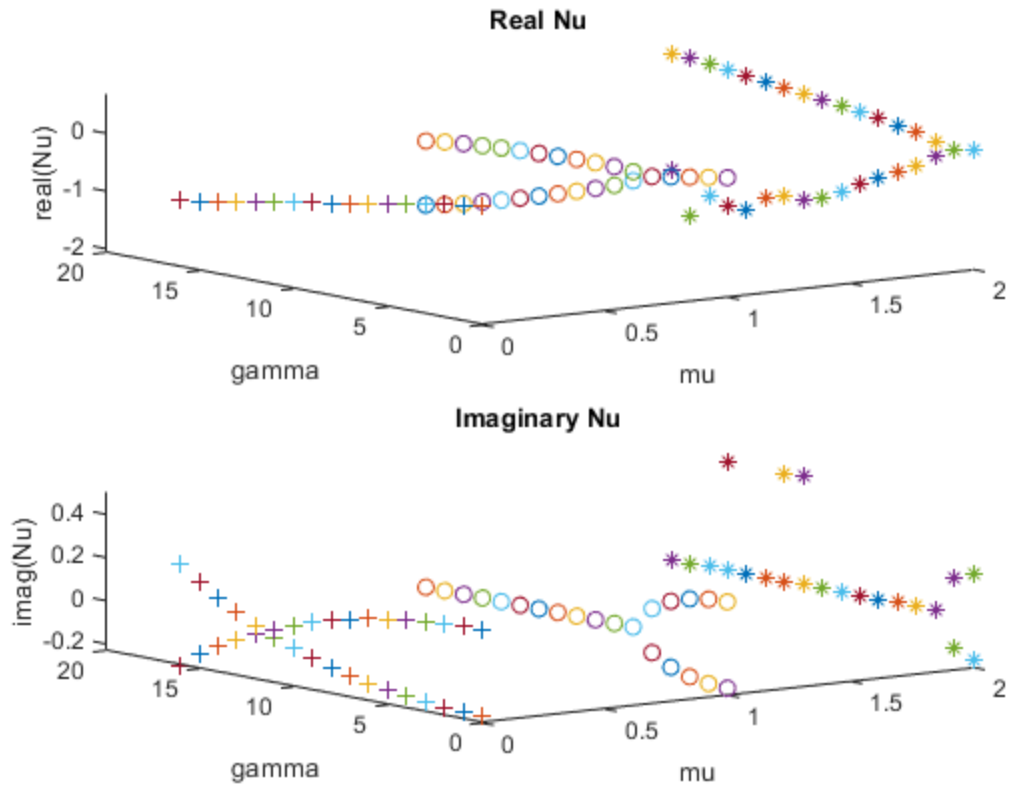
1 1 1 1 1 1 1 1 1 1 1 1  
 1 1

Columns 27 through 39

1 1 1 1 1 1 1 1 1 1 1 1  
 1 1

Columns 40 through 51

1 1 1 1 1 1 1 1 1 1 1 1  
 1



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