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DNA Mapping Algorithms: Abstract Data Types - Concepts and Implementation

Will Gillett and Liz Hanks

The conceptual aspects of and the implementation details of a set of self-identifying abstract data types (ADT) are described. Each of the ADTs constitutes a specific class of object, upon which a set of well-defined access functions is available. The intent of these ADTs is to supply a paradigm in which a class of object is available for manipulation, but in which the underlying implementation is hidden from the application programmer. Specific ADTs are the described in some detail. The tagged architecture used to achieve the self-identifying property of the ADTs is presented, and a set of required system-backbone... Read complete abstract on page 2.

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DNA Mapping Algorithms: Abstract Data Types - Concepts and Implementation

Will Gillett and Liz Hanks

Complete Abstract:

The conceptual aspects of and the implementation details of a set of self-identifying abstract data types (ADT) are described. Each of the ADTs constitutes a specific class of object, upon which a set of welldefined access functions is available. The intent of these ADTs is to supply a paradigm in which a class of object is available for manipulation, but in which the underlying implementation is hidden from the application programmer. Specific ADTs are the described in some detail. The tagged architecture used to achieve the self-identifying property of the ADTs is presented, and a set of required system-backbone access function is defined. Their combination is shown to produce a robust system in which complex aggregate ADT classes can be flexibly created and managed with little effort on the part of the application programmer. Memory management and statistics reporting techniques are presented.

DNA Mapping Algorithms: Abstract Data Types -**Concepts and Implementation**

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WUCS-91-33

June 1991

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ABSTRACT

The conceptual aspects of and the implementation details of a set of self-identifying abstract data types (ADTs) are described. Each of the ADTs constitutes a specific class of object, upon which a set of well-defined access functions is available. The intent of these ADTs is to supply a paradigm in which a class of object is available for manipulation, but in which the underlying implementation is hidden from the application programmer.

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1. Introduction

This reports describes the conceptual aspects of and the implementation details of a set of selfidentifying abstract data types, which will be referred to here as ADTs. Each of the ADTs constitutes a specific class of object, such as integer, list, or tree, upon which a set of well-defined functions should be applicable. The intent of ADTs is to supply a paradigm in which a class of object is available for manipulation, but for which the underlying implementation is hidden from the application programmer.

The DNA Mapping encapsulation of ADTs, as implemented with a self-identifying (tagged) architecture, constitutes a paradigm very similar to that of object-oriented programming (OOP). The major difference between standard object-oriented programming and the DNA Mapping ADTs is that inheritance is present in most object-oriented system but is not present in our ADTs.

1.1. Software Engineering Reasoning for ADTs

Although the underlying implementation of ADTs is based on a combination of standard, wellunderstood data structures (arrays, structs, pointers, and intrinsic data types), the application programmer is not allowed to know this underlying structure or access any of the actual physical components directly. Instead, a set of access functions is supplied, with which the application programmer can manipulate the conceptual components of an ADT.

For instance, given an ADT intended to simulate a list of objects, adt list, the application programmer may want to know the cardinality of a specific list. In order to extract this information, an access function, say list cardinality, would be supplied. When invoked, this function would return the number of objects currently in the list -- but without the application programmer knowing how the underlying implementation is achieved. For example, it might be that the cardinality is actually held as an explicit field of the underlying data structure representing the conceptual list, and list cardinality simply references this field causing no computation to be done. In this case the cardinality field probably would be incremented each time an object is inserted into the list and decremented each time an object is deleted from the list. This underlying implementation requires an explicit memory location to maintain the datum continually being updated. An alternative approach is not to maintain explicit information about the cardinality, but instead to search through the list, counting the number of objects present each time the list cardinality function is invoked. This implementation option requires no extra memory to hold the explicit cardinality. Each has its own advantage. One is efficient in time, and the other is efficient in space.

Another option for holding lists is to implement them either as a sequential array or as a dynamically allocated linked list. Each of these possibilities has its advantages and disadvantages. The linked list approach may be efficient in time with respect to insertions and deletions, but may take much more memory than the array approach. The array approach may be efficient with respect to memory, but has severe time penalties for insertion and deletion of objects and may require significant reallocation as the list grows in size.

The ADT paradigm claims that all of these underlying implementation decisions should be hidden from the application programmer. The question as to why this is an desirable property to have is an appropriate and important one. The basic answer is the following. The application programmer should program in a conceptual space that does not change unless the application itself changes. In other words, the "things" manipulated by the programmer should be perceived to be "things" that are important to the application and not primarily important to the details of some specific programming language (i.e., "things" that are important to the solution of the application). Once the solution to a problem (application) has been found, it should not have to be changed just because something in the underlying implementation changes. (A more global example of this has to do with the reason that high-level languages are used to solve problems. Specifically, if a solution to a problem has been found using the language C, then we would like that solution to remain applicable even though the eventual executable program is run on a machine other than the one upon which it was developed.) In the conceptual world of ADTs, we would like the solution to a

problem to remain valid, even though the underlying implementation of a list is changed from an array approach to a linked list approach. Specifically, with respect to the application, the sequence of insertions into and deletions from some list will be identical, independent of the mechanism chosen to implement the list (i.e., array or linked list). If, for some reason, the original mechanism chosen for implementing lists is found to be inappropriate or deficient and a subsequent decision is made to change the original mechanism for implementing lists, the application code itself should not have to be changed just because the underlying implementation of lists has changed.

By hiding the underlying implementation of the ADTs, implementation decisions can be deferred or changed without affecting the quality or validity of the application code being developed. This allows prototype systems to be developed quickly. If a quick-and-dirty but inefficient initial implementation of a set of ADTs can be created, then it may be possible to create the basic functionality of an application quickly, allowing the fine-tuning and time and space optimization to be deferred until later in the project.

Besides the ability to change the underlying implementations of the ADTs without affecting the application code built upon them, simply the use of mathematically well-understood abstractions (implementable as ADTs) is an extremely powerful conceptual tool in the programming of solutions to applications. If ADTs simulating lists, sets, pairs, trees, stacks, etc. can be implemented, then the application programmer can use these powerful conceptual tools as actual tools available in the concrete form of programming constructs. Specifically, many problems themselves are described by using abstract mathematical concepts. More importantly, abstract algorithms for solving the problems are often expressed using these abstract mathematical concepts. The ability to implement an abstract algorithm quickly, without resorting to time-consuming translation into standard mundane programming constructs, makes it possible to determine the validity of ideas quickly. It also enhances the ability to change, reconfigure, upgrade, manage, document and verify the application code produced.

At the inception of the DNA Mapping project, it was clear that whatever specific code was produced at the start of the project would not be applicable by the end of the project, let alone years after the end of the project. This is true for a myriad of reasons. The biological laboratory protocols will change over time; the problems themselves will change over time; the questions being asked by the biologist will change over time. It was evident that whatever code was produced would have to be extremely reconfigurable in order to adapt to (a) changes whose origin and nature are already known but whose specifics are not currently known and (b) changes whose origin and nature cannot be anticipated. The incorporation of ADTs within the system has largely been due to this realization. It is hoped that by the use of very abstract high-level constructs, large components of the software will be extractable, modifiable, and reusable over a long period of growth and learning about DNA mapping.

1.2. Self-identifying Properties of ADTs

The self-identifying properties of the ADTs implemented within the system are paramount to the operation of the system, because they allow the type of an object to be determined at execution time instead of at compile time. The self-identification is achieved by attaching a tag to each instance of an ADT at execution time. Each instance of an ADT in a specific class of ADT is given the same tag as all other instances in that class of ADT. The tags used across the different classes of ADTs are uniquely different, i.e., the tag of an instance uniquely identifies the class of ADT to which the instance belongs. This tag is not a compile-time concept; it is an execution-time concept. It is present and identifiable at execution time. This means that, given a pointer to an arbitrary instance of an ADT, it is possible to determine the class of ADT to which it belongs at execution time.

This self-identifying property of ADTs allows combinations (or aggregates) of ADTs to be put together in arbitrary ways. For instance, it is possible to create a list that contains objects which are instances from different classes of ADTs. In other words, a list can have a combination of objects present in it, such as integer ADTs, float ADTs, and string ADTs. The ADT classes are not restricted to intrinsic data types, however. A list can contain another list as one of the objects present in it. In fact, there is no limit to the recursive inclusion of ADTs as components of other ADTs. For instance, it is possible to have a pair whose left element is a string ADT and whose right element is a list of trees. It also is possible to have a list of stacks of pairs of trees.

The use of ADTs with an execution-time tag present does restrict what can be generically used as components of ADTs. In most cases, the generic components must be ADTs themselves. In other words, raw (unencapsulated) C data types such as integer, float, and string are not allowed, since they have no tag present to identify their type at execution time. This does present minor restrictions on the use of ADTs. In general the solution to these restrictions is to "wrap" raw intrinsic C data types into an ADT and use the ADT counterparts as components of other (aggregate) ADTs. These ADT classes are supplied for: integer, float, string, and Boolean.

1.3. System-backbone Access Functions

For each ADT class, a set of required system-backbone access functions must be supplied. Each ADT class is declared to the system at execution time; these required access functions are made available to the system at this declaration time. They include (a) how to create an instance of the ADT, (b) how to destroy an instance of the ADT (i.e., return the, possibly aggregate, memory associated with the instance). (c) how to make a copy of an instance of the ADT, (d) how to pretty print an instance of the ADT (i.e., print the contents of the instance in a high-level conceptual manner), (e) how to debug print an instance of the ADT (i.e., print the contents of the instance in a low-level detailed manner), and (f) how to compare two instances of the ADT to determine whether one is less than, equal to, or greater than the other.

Given these access functions and the self-identifying properties of the ADTs, the application programmer can manipulate aggregate ADTs in very generic ways. For instance, the programmer can pretty print a list by calling the routine list pprint. In this process, appropriate punctuation (square brackets and a comma) are used to delimit the objects in the list, as one might expect. However, the actual printing of the objects themselves cannot be accomplished by the list pprint routine directly because it does not have the knowledge required to pretty print every type of object present in the system. Instead, since the tag of each object is available at execution time, the appropriate pretty print routine applicable to the specific object present can be "looked up" and invoked to produce the desired results.

Similar logic holds for destroying, copying, debug printing and comparing compound objects. In fact, since this idea of recursively operating on a compound object (based on the tag of its components) is so pervasive that macros which accept an object and call the appropriate specific function based on the value of the tag found are supplied to the application programmer. These macros include DESTROY, COPY, PPRINT, DPRINT, and COMPARE.

The ideas used for building complex data structures using these types of ADTs are very similar to those used while producing complex data structures in LISP. In LISP, whenever a list of objects is desired, a left-spined or right-spined tree is created with the objects "hanging" from the tree; here a specific generic list is created. However, the application programmer need put no effort into understanding or implementing the details of the list mechanism. In LISP, if a pair of objects is desired, a cons is performed making one object the left son of a tree and the other object the right son of the tree; here an explicit pair is created. In general the conceptual viewpoint for creating complex data structures using ADTs is similar to that found in using LISP

1.4. Exposition

In order to expose the nature of the ADTs present in the system, the details of four specific ADTs will be presented: adt int (integer), adt string (character string), adt pair (a 2-tuple), and adt dll (doubly-linked list). adt int is included because it is a very simple fixed-size intrinsic data type. adt string is included to show the variation involved for a variable-length data type. adt_pair is included because it is probably the simplest aggregate ADT present in the system. adt dll is included to show the complexity of a variable-length, multiple-component ADT.

The reader should be aware that the code presented in this report is not exactly the same as that present in the DNA Mapping software. In general, the code shown here is intended to convey the important ideas and some of the details of ADTs. However, the code has been simplified to eliminate system detail that might confuse this exposition.

The reader also should be aware that the use of ADTs does have some disadvantages. The power of these ADTs allows the application programmer to do many unorthodox and inappropriate things. For instance, it is possible to include as a member of a list the list itself (since actual pointers are used). If such a hideous recursive situation occurs, an action as simple as a pretty print will produce infinite output. Since memory is dynamically allocated in creating ADTs and the user of the ADT is responsible for destroying the ADT (i.e., returning the memory), the application programmer must be vigilant to destroy each instance of an ADT which is no longer needed. Failure to comply with this maxim will cause memory exhaustion and the execution will abort. Consider the prospect of leaving just one word of memory inappropriately allocated in the middle of a loop which is executed a million times.

Section 2 presents a number of required system-backbone access function that must be present for every ADT class declared to the system. The presence of these functions along with the self-identifying property of the ADTs allows the effective management of complex aggregate ADTs. Section 3 shows how to implement the normal object-operation access functions associated with ADTs. Section 4 describes how an ADT class is declared to the system at execution time, how statistics about the status of instances of ADTs can be obtained, and how memory management is performed. Section 5 briefly describes a set of ADTs present in the DNA Mapping system. These ADTs are subdivided into three categories based on their generality. Section 6 discusses the usefulness and utility of the ADT paradigm.

2. Required System-backbone Access Functions

In order to use an ADT within the system, it must first be declared to the system. In this declaration a number of required system-backbone access function are made available to the system, the size of an instance is given, the pointer to the null object is specified, and the tag to be used for this ADT is returned for external use. The details of this declaration will be deferred to Section 4.1. Here, we are interested in the access functions that are presented during this declaration. They are the following functions: create, destroy, pprint, dprint, copy, and compare.

2.1. Creating

As a simple introduction to creating an instance of an ADT, consider adt int. Assume that the structure of an adt int has been declared as in Figure 1. In this figure, the macro MEM NULL refers to the NULL pointer for a generic ADT of unknown class; its current value is 0 in compliance with most null pointers. The macro INT VAL is used to mask the underlying implementation from the programmer. Note that, in this case, the programmer is not the application programmer but instead the creator of the ADT class itself. Such hiding by macros has been found to be invaluable for allowing structural changes to

```
struct int node {
            int int fld;
        \cdottypedef struct int node
                            STR INT TYPE, *INT TYPE;
#define INT_NULL ((INT TYPE)MEM NULL)
#define INT VAL(p) ((int)(p)->int_fld)
```
Figure 1: Declarations for adt int

occur to the underlying implementation while minimizing the amount of code that must be modified.

A simple routine for creating an instance of an adt int can be constructed, as shown in Figure 2. In this type of create routine, the actual value of the desired ADT is presented at creation time. This is simple because the value being inserted into the ADT is a scalar, in contrast to creation of an aggregate list. Here, the integer i is an input parameter. The first executable statement simply insures that initialization (mostly declaration) has been done. The invocation of mem man fixedsize allocate allocates the correct amount of memory for a data structure of this class. (Here, the prefix mem man stands for "memory management".) The details of this will be deferred to Section 4.3.1. However, the general idea will be discussed here. In this case, two full words of memory are allocated; one for the tag and one for the integer itself. (The size of the adt int is known to the system because it was declared at initialization time and thus need not be specified here. This is in contrast to a variable-size data structure, in which a call to mem man varsize allocate will be performed.) The correct tag for an adt int is placed in the first word of the memory allocated, and a pointer to the second word (the actual adt int structure as declared in Figure 1) is returned through the function name. The macro INT VAL is used to insert the value of the input parameter into the memory which has been allocated. A pointer to the user-accessible portion of this instance of an adt int is returned through the function name.

In this ADT convention, the system knows that if it is manipulating a pointer to an instance of an ADT, then it can find the tag corresponding to this instance one word to the left of the current pointer. However, the current pointer points to exactly the structure which was declared by the programmer. Thus, this pointer can be used as if there were no tag present at all.

Now consider a more complex situation in which a variable amount of memory must be allocated based on the "size" of the incoming argument. Such a situation is typified by adt_string. Consider the declarations of Figure 3. Here, notice that the struct string_node actually contains no space for the

```
INT TYPE
int create(i)
    int i;\overline{\mathbf{t}}INT TYPE
                  p;if(!int init done) int ds init();
    p = (INT TYPE) mem man fixedsize_allocate(int tag);
    INT VAL(p) = i;
    return(p);1
```

```
Figure 2: Creation of an Instance of adt int
```

```
struct string node{
            int size fld;
        \cdottypedef struct string node STR STRING_TYPE, *STRING_TYPE;
#define STNG NULL
                  ((STRING TYPE) MEM NULL)
#define STNG SIZE(p) ((int)(p)->size fld)
#define STNG VAL(p) ((STRING)((MEM TYPE)(p)+sizeof(STR STRING TYPE)))
#define STNG LEN(p)
                      ( (int) strlen (STNG VAL(p)))
#define STNG IS EMPTY(p)
                            (STNG LEN(p) == 0)
```
Figure 3: Declarations for adt string

variable-size string that eventually will reside in the instance of the adt string. Instead there is only an integer size fld (size field) which will be used to indicate the size of the (user-specified) variable-size memory allocated for this instance of the adt string. The actual string data will be concatenated just after this one-word field. Note again the use of macros to mask the underlying implementation.

The code for creating an instance of an adt string is shown in Figure 4. Here, the type STRING is equivalent to char \star . The structure of the code here is similar to that of Figure 2, but there is some variation. The length of the (user-specified) portion of the data structure must be computed. This is the length of the character string (i.e., the call to $strlen$) plus 1 (for the $\setminus 0$ at the end of the string) plus the length of the size fld itself. The correct amount of memory is allocated by calling mem man varsize allocate. Note that in this variable-size case, the size of the desired object must be specified (as the second argument, size). The size fld is set by using the STNG SIZE macro. Then the value of the incoming string is copied to just after the size fld component of the struct. The pointer to the (user-specified) data structure is returned through the function name.

Several conventions have been used here that are important to the construction of ADTs. It should be clear that there are two routines used for allocating memory: mem man fixedsize allocate for fixed-size ADTs, and mem man varsize allocate for variable-size ADTs. Correspondingly, there are two deallocation functions: mem man fixedsize deallocate and mem_man_varsize_deallocate. For fixed-size ADTs there is no question about how much memory to deallocate when an instance is returned to the system. However, for the deallocation of a variable-size ADT, the original amount of memory allocated at creation time must be specified at destruction time, so that the correct amount of memory is returned. This is the basic reason for the including the size fld in the structure of an adt string. It's value will be used at deallocation time. The decision to make it the first field of the struct is an important one. This is because there are two ways of returning an instance of a variable-size ADT to the system. mem man varsize deallocate may be called, in which case the size of the (user-specified) data structure must be specified. Alternatively mem man fixedsize deallocate can be called if the builder of the ADT class has used the convention to make the size of the variable-size data structure the first field of the data structure. In this case, if the instance is known to be of variable length, mem_man_fixedsize_deallocate simply looks in the first field of the structure for the appropriate length and deallocates that amount of memory.

Now consider an aggregate ADT, adt pair, which implements a 2-tuple. The declarations for an adt pair are shown in Figure 5. Here again, the standard use of macros masks the underlying structural implementation.

```
STRING TYPE
string create (s)
    STRING
                  s;\mathfrak{f}STRING TYPE
                      Pint
                  size;
    if(!string init done) string ds init();
    size = sizeof(STR STRING TYPE) + strlen(s) + 1;p = (STRING TYPE) mem man varsize allocate (string tag, size);
    STNG\_SIZE(p) = size;strcpy (STNG VAL(p), s);
    return (p);
\mathbf{I}
```

```
struct pair {
    MEM TYPE left element fld;
    UTIL TYPE left util fld;
    MEM TYPE right element fld;
    UTIL TYPE right util fld;
\} ;
typedef struct pair STR PAIR TYPE, *PAIR TYPE;
#define PAIR NULL (PAIR TYPE) MEM NULL
#define PAIR LEFT ELEMENT (p)
                               ((MEM TYPE)(p)->left_element_fld)
#define PAIR RIGHT ELEMENT (p) ((MEM TYPE) (p) ->right_element_fld)
#define PAIR LEFT UTIL(p)
                                ((p) - \lambda left util fld)
#define PAIR RIGHT UTIL(p)
                                ((p)->right util fld)
#define PAIR IS EMPTY(p)
                                (PAIR LEFT ELEMENT (p) == MEM NULL \&\&PAIR RIGHT ELEMENT (p) == MEM NULL)
```
Figure 5: Declarations for adt pair

Note that in the declaration of the struct pair, there are more than two fields, i.e., more than just the left element fld and the right element fld. The two extra fields are referred to as utility fields, and indicate whether or not the corresponding component object should be destroyed in the process of destroying the pair itself. This idea of "destroyable or not" comes from the concept of "ownership". Specifically, certain aggregate ADTs will deal with managing data (i.e., objects) for some other application. If the ADT is just managing data, then it does not "own" the data itself, and therefore when it (in this case, the pair) is destroyed and its management activities end, it should not destroy the data that it was managing because some other application "owns" the previously managed data and needs to manipulate it more. If the destruction of the managing pair caused the destruction of the data it is managing, then the application requesting the management would not operate correctly because its data would have been destroyed. The field left util fld is a BOOLEAN which indicates whether or not the object held in the field left element fld is "owned" by this instance of an adt pair, i.e., whether or not the object held in the field left element fld should be destroyed when this instance of an adt pair is destroyed. The field right util \overline{f} ld is a BOOLEAN which indicates whether or not the object held in the field right element fld is "owned" by this instance of an adt pair, i.e., whether or not the object held in the field right element fld should be destroyed when this instance of an adt pair is destroved.

This kind of utility "ownership" field is present in many of the aggregating ADTs, such as list and set. Often, there are additional separate access functions for inserting objects into aggregate ADTs, for which the component objects being managed should not be destroyed when the aggregate ADT itself is destroyed. These access functions will contain the string " ddd" as part of the name of the access function. The ddd is meant to connote "don't destroy data". Thus, a call such as pair_create_ddd(obj1,obj2) creates an instance of an adt pair in which obj1 and obj2 will not be destroyed when the managing pair itself is destroyed, whereas a call such as pair create $(obj1, obj2)$ creates an instance of an adt pair in which obj1 and obj2 will be destroyed when the aggregating pair itself is destroyed. In the case of the adt pair there also are access functions for selectively allowing either the right or left field to be destroyed or not.

The code for creating an adt pair is shown in Figure 6. Notice that the type of the input parameters is MEM TYPE. This is the generic type for an ADT of unknown class. Since the ADT class of the objects that will be placed in the pair at execution time cannot be known at compile time, MEM TYPE is the only appropriate type for the input parameters. The constant UTIL CAN DESTROY is used to indicate that the object held in the corresponding field should be destroyed when the pair created here is destroyed. There is a corresponding UTIL CANT DESTROY constant. To show the variations possible for utility management, the code for pair create ddd left is shown in Figure 7. Notice that the flag indicating whether or not a component object should be destroved can be modified after creation of the aggregating object.

```
PAIR TYPE
pair create(left, right)
      MEM TYPE left, right;
\mathfrak{f}PAIR TYPE a;
    if (!pair_init_done) pair_ds_init();
    a = (PAIR_TYPE) mem_man_fixedsize_allocate(pair tag);
    LEFT ELEMENT (a) = left;
    RIGHT ELEMENT (a) = right:util set destruction (&PAIR LEFT UTIL(a), UTIL CAN DESTROY);
    util set destruction (&PAIR RIGHT UTIL(a), UTIL CAN DESTROY);
    return(a);\, }
                       Figure 6: Creation of an Instance of adt pair
PAIR TYPE
pair create ddd left (left, right)
      MEM TYPE left, right;
\mathfrak{f}PAIR TYPE a;
    a = pair create(left, right);util set destruction (&PAIR LEFT UTIL(a), UTIL CANT DESTROY);
    util set destruction (&PAIR RIGHT UTIL(a), UTIL CAN DESTROY);
    return(a);\mathbf{I}
```
Figure 7: Code for pair create ddd left

The last ADT class to be addressed is the adt dll. Declarations used in the definition of the adt dll are shown in Figure 8. The adt dll is based on the concept of a list node. In fact, there is a separate ADT class for list node with its own access functions. Its direct implementation will be suppressed here, and it will be assumed that the reader can infer the meaning of any access function that occurs in the code from the name of the access function itself.

In the declaration of a list node there are three major fields: the left fld, the right fld, and the data fld. The left fld of a node points to the node to its left. Similarly for the right fld. The data fld points to the instance of the ADT being held at this position. There are two other minor fields. The util fld is used to indicate ownership, and specifies whether or not the object pointed to by the data fld of this node should be destroyed when this node is destroyed. The up fld indicates the context in which this node resides. It is essentially a "parent" indicator. In most cases this field points to the header node of the adt dll in which it resides.

An adt dll implements a doubly linked list with a header. The empty adt dll contains one and only one node, the header node; the left fld and the right fld point to the header node itself. The header node is distinguished from all other list nodes in that the data fld of the header node points to the header node itself.

The code for creating an instance of an empty adt_dll is shown in Figure 9. Notice that the implementation style here is exactly the same as the previous creation routines. However, in this case the corresponding object being created is the empty object. Also, note the introduction of the concept of a

struct list node { MEM TYPE up fld; *left_fld; struct list node struct list_node *right fld; MEM TYPE data fld; UTIL TYPE util fld; \mathcal{F} typedef struct list node STR LIST NODE TYPE, *LIST NODE TYPE; typedef STR LIST NODE TYPE STR_DLL_TYPE, *DLL_TYPE; #define DLL NULL (DLL TYPE) PNT LIST NODE NULL #define DLL LEFT(p) $($ (LIST NODE TYPE) (p) -> left fld) #define DLL RIGHT(p) ((LIST NODE TYPE) $(p) \rightarrow$ right fld) $((MEM TYPE) (p) -> data fld)$ #define DLL DATA(p) #define DLL PARENT(p) $(MEM$ TYPE) (p) -> up fld) #define DLL UTIL(p) $((MEM TYPE) (p) -> util fd)$ #define DLL_IS_HEAD(p) $(DATA(p) == (MEM TYPE) (p))$

Figure 8: Declarations for adt dll

```
DLL TYPE
dll_create(parent)
    MEM TYPE
                     parent;
\{DLL_TYPE
                 pif (!dll_init done) dll ds init();
    p = (DLL TYPE) mem man fixedsize allocate (dll tag);
    LEFT(p) = p;
    RIGHT(p) = p;
    DATA(p) = (MEM TYPE)p;
    PARENT(p) = parent;
    return(p);\mathbf{I}
```
Figure 9: Creation of an empty adt_dll

"parent" to indicate the context in which the specific instance of the adt dll resides.

2.2. Destroying

The concept of destroying an object deals with returning the memory, which was allocated for "holding" that object, to the system for future used by other instances of ADTs. Since no part of the application should have a pointer to this returned memory after deallocation, whatever variable is used to hold the pointer to this object (in order to return the memory to the system) should be NULLed out after the destroy has been completed. In order to help enforce this convention, a pointer to the pointer to the object is handed to the destroy function, and it is the responsibility of the destroy function to NULL out the pointer it received upon completion of the return of the memory.

Consider the destruction of an adt int, as shown in Figure 10. Here, note the call to mem_man_fixedsize_deallocate. Since this is a fixed-size data structure, the system knows the amount of memory that was allocated and therefore how much to deallocate. Thus, there is no need to supply the data structure size for deallocation. Note that a pointer to the pointer to the data structure is passed to this routine. The pointer to the data structure is set to NULL, just before returning.

```
void
int destroy (p)
        INT TYPE
                         *_{p}\mathfrak{f}if (*p == INT NULL) return;
        mem man fixedsize deallocate ((MEM TYPE) *p);
        *_{\mathcal{D}} = \text{INT NULL};return;
\mathbf{)}
```
Figure 10: Destruction of an Instance of adt int

When destroying a variable-size object, only slight differences occur. Consider the destroy of an adt_string, as shown in Figure 11. Notice here that there is a calculation of the size of the memory which must be returned and the call to mem man varsize deallocate with a second argument which specifies that size.

Notice that there are no component ADTs to be destroyed in the adt int and the adt string. For an example of an aggregate ADT which has component ADTs which may have to be destroyed, consider the destroy of an adt pair, as shown in Figure 12. Here, the routine determines ownership by checking to see if it should destroy its two component objects. Any component that should be destroyed is destroyed, and then the memory for the pair itself is returned to the system.

As the last example of a destroy routine, consider the destroy of an adt dll, as shown in Figure 13. Here, each list node in the adt dll is selected and destroyed. The check to determine ownership is "hidden" in the call to list node destroy. Notice that it is possible that some of the objects placed in the adt dll may be destroyable and other may be nondestroyable. A selective decision is made at each list node as to which component objects are destroyable and which are not. After each of the nodes in the list has been destroyed, the memory for the header node is returned to the system.

In the destruction of an adt pair and an adt dll, the macro DESTROY has been used. This macro interrogates the tag of the object handed to it to determine which specific destroy routine should be used to return the appropriate amount of memory to the system. It should now be clear why the execution-time tagged architecture is so important to the effective use of recursively embeddable ADTs. Without the

```
void
string destroy (p)
       STRING TYPE *p;
\mathfrak{f}intsize:if (*p == STNG NULL) return;
       size = STNG SIZE(*p);mem man varsize deallocate ((MEM TYPE)*p, size);
       *_{\mathcal{P}} = STNG NULL;
       return;
ł
```


```
void
pair destroy (pair)
    PAIR TYPE
               *pair;
\{if (*pair == PAIR NULL) return;
    if (util can destroy (&PAIR LEFT UTIL (*pair)))
        if (LEFT ELEMENT (*pair) != MEM NULL)
            DESTROY (&LEFT ELEMENT (*pair));
    if (util can destroy (&PAIR RIGHT UTIL (*pair)))
        if (RIGHT ELEMENT (*pair) != MEM NULL)
            DESTROY (&RIGHT ELEMENT (*pair));
   mem_man_fixedsize_deallocate((MEM_TYPE)*pair);
    *pair = PAIR NULL;
    return:
}
```
Figure 12: Destruction of an Instance of adt pair

```
void
dll destroy (dll)
    DLL TYPE
                *d11;\{LIST NODE TYPE ln;
    if (*d.l = D.L NUL) return;
    ln = RIGHT(*dll);while (!DLL IS HEAD(ln)) {
        list node destroy (&ln);
        ln = RIGHT(*dll);\cdotmem man fixedsize deallocate ((MEM TYPE) *dll);
    *d11 = DLL NULL;return;
}
```
Figure 13: Destruction of an Instance of adt dll

execution-time tag present, it would be impossible to correctly manipulate (in this case, deallocate memory) the constituent components of a complex aggregate ADT.

2.3. Pretty Printing

The objective of pretty printing is to have the logical content of an instance of an ADT printed in a high-level manner, from which the reader can quickly extract the content. For scalar objects, this is relatively straightforward. Consider the code for int_pprint as shown in Figure 14. Notice that the logic is extremely simple. The integer value is extracted and printed. No new-line is printed; this is because the pretty print of the integer may be done in a much larger context, that of an aggregate ADT. Extraneous new-lines may destroy the overall contextual effect desired. Here, the macro RERROR prints an error message. The first argument to the macro, ABORT CODE, indicates that this is a severe error, and after printing the error message the run should be aborted.

```
void
int_pprint(p)
       INT TYPE
                    p:\mathfrak{t}int
             \pm;
      if (p == INT_MULL) RERROR(ABORT CODE, ("NULL pointer"));
      i = INT VAL(p);printf("d", i);return;
\, }
```
Figure 14: Pretty Print of an Instance of adt_int

The pretty print of a variable-size object is not much different, as shown in the code for string pprint in Figure 15.

The pretty print of an aggregate ADT requires some punctuation. In the case of the adt pair, the two objects of the 2-tuple are place between parentheses, with a comma between them. The pretty print routine for an adt pair, pair pprint, is shown in Figure 16. Note the use of the macro PPRINT to perform the pretty print on the two components, the types of which are unknown. Notice again that no new-line is printed which might destroy the contextual effect.

The pretty print for the adt dll is shown in Figure 17. Note the call to list node pprint to achieve the pretty printing of the object at each selected position of the list.

In order to see the utility of the tag architecture and the declaration of the required system-backbone routines, now consider the code shown in Figure 18(a), which produces a relatively complex ADT structure. This code first creates an adt dll containing two elements, the string "abc" and the integer 1. It then creates an adt pair containing this adt dll as its first element and the integer 2 as its second element. It then creates a second adt dll, whose first object is the pair just created and whose second object is the string "def". The resulting ADT is pretty printed, and the output produced is shown in Figure 18(b).

```
void
string pprint (p)
       STRING TYPE
                                p.
\mathbf{f}STRING
                                S:
       if (p == STNG NULL) RERROR(ABORT CODE, ("NULL pointer"));
       s = STNG VAL(p);
       printf(\sqrt[n]{s} \sin n, s);
       return;
\overline{\mathbf{r}}
```
Figure 15: Pretty Print of an Instance of adt string

```
void
pair_pprint(pair)
     PAIR_TYPE
                     pair;
\mathfrak{f}% _{0}\left( t\right) \equiv\mathfrak{f}_{0}\left( t\right) ,if (pair == PAIR_NULL) RERROR(ABORT_CODE, ("NULL pointer"));
     print(f(" "));
     PPRINT (LEFT_ELEMENT (pair));
     print(f'','');
     PPRINT (RIGHT_ELEMENT (pair));
     print(f("));
     return;
\mathcal{Y}
```
Figure 16: Pretty Print of an Instance of adt pair

```
void
dll_pprint(dll)
    DLL_TYPE
                 dll;
\overline{1}LIST_NODE_TYPE ln;
    if (dll == DLL_NULL) RERROR(ABORT_CODE, ("NULL pointer"));
    ln = RIGHT(dll);print(f("<");
    while (!DLL IS HEAD(ln) {
        list_node_pprint(ln);
        ln = RIGHT(ln):
    \mathbf{E}print(f(">");
    return;
\mathbf{E}
```
Figure 17: Pretty Print of an Instance of adt dll

```
d111 = d11 create (MEM NULL);
dll insert data to right (dll1, dll1, int create (1));
dll insert data to right (dll1, dll1, string create ("abc"));
pair = pair create(dlll, int create(2));d112 = d11 create (MEM NULL);
dll_insert_data_to_right(dll2,dll2,string create("def"));
dll insert data to right (dll2, dll2, pair);
d11 pprint (d112);
```
 (a)

 $\langle \langle 4 \rangle$ < $\langle 4 \rangle$ + $\langle 1 \rangle$, $2 \rangle$, "def">

 (b)

Figure 18: Example Input and Output for Pretty Print

2.4. Debug Printing

The objective of debug printing is to have the implementation content of an instance of an ADT printed in a low-level manner, from which the reader can extract the details of the implementation. This is for the purpose of discovering errors in the implementation. The overall idea behind debug printing is similar to that of pretty printing except that all the implementation details, such as explicit pointers into memory, are displayed.

Consider the debug printing for an adt int, as shown in Figure 19. Notice that the value of the integer stored as well as the pointer to the memory at which it is stored are printed. Similar code is used for debug printing an adt string, as shown in Figure 20.

A debug print for a simple aggregate ADT such as an adt pair has a similar structure to its pretty print counterpart, as shown in the code for pair_dprint presented in Figure 21. Notice the recursive use of the macro DPRINT.

In order to keep things simple for complex aggregate ADTs, such as an adt dll, the unbounded complexity of the structure is suppressed, as shown in the code for dll dprint presented in Figure 22. Here, only the fields of the header node are printed in detail. The reason for simplifying the debug printing of a complex ADT such as this is as follows. The basic reason for doing a debug print is to find an error;

```
void
int_dprint(p)
      INT TYPE
                    p,
ł
      int
             \pm;
      if (p == INT NULL) RERROR(ABORT CODE, ("NULL pointer"));
      i = INT VAL(p);print(f("(intfx(i:\d))", p, i);
      return;
\mathbf{I}
```
Figure 19: Debug Print of an Instance of adt int

```
void
string dprint (p)
       STRING TYPE
                           P:\{if (p == STRING NULL) RERROR(ABORT CODE, ("NULL pointer"));
      printf ("(str%x(sz:%d)(s:\"%s\"))", p, STNG SIZE(p), STNG VAL(p));
       return;
\mathcal{E}Figure 20: Debug Print of an Instance of adt string
void
pair dprint (pair)
    PAIR TYPE
                 pair;
\{if (pair == PAIR NULL) RERROR(ABORT CODE, ("NULL pointer"));
```

```
print(f("));
    DPRINT (LEFT ELEMENT (pair));
    print(f'',");
    DPRINT (RIGHT_ELEMENT (pair));
    print(f("));
    return;
\mathbf{E}
```
Figure 21: Debug Print of an Instance of adt_pair

```
void
dll_dprint(dll)
    DLL TYPE
                   dll:
\left\{ \right.if (dll) == DLL NULL RERROR (ABORT CODE, ("NULL pointer"));
    printf ("dl1%x (u:%x) (1:%x) (r:%x)) ",dll, PARENT(dll), LEFT(dll), RIGHT(dll));
    return;
\mathbf{)}
```
Figure 22. Debug Printing of an Instance of adt dll

usually this error involves an erroneous pointer. The process of debug printing should not produce an error in its own right. If one of the pointers in a list node is in error, then a debug print routine which follows that erroneous pointer may cause an execution error. In order to eliminate this kind of "random search" through memory, only the top-level header node is debug printed. During debugging, it is possible to "march down" the separate list nodes of the adt dll to discover the pointer error.

The code shown in Figure $23(a)$ produces the debug print output shown in Figure $23(b)$.

```
d111 = d11 create (NULL);
int1 = int create(1);
int dprint (intl);
dll_insert_data_to_right(dll1,dll1,int1);
stringl = string create ("abc");
string dprint (stringl);
dll_insert_data_to_right(dll1,dll1,string1);
d11 dprint (d111);
int2 = int create(2);
int dprint (int2);
pair = pair create(dlll, int2);pair dprint (pair);
d112 = d11 create (NULL);
string2 = string create("def");
string dprint (string2);
dll_insert data to right(dll2,dll2,string2);
dll_insert_data_to_right(dll2,dll2,pair);
dll dprint (d112);
```

```
(a)
```

```
(int2198b1(i:1))(str21988d(sz:8) (s: "abc") )(d11219828(u:0) (1:2197e8) (r:219899))(int2198f5(i:2))((d11219828(u:0)(1:2197e8)(r:219899)), (int2198f5(i:2)))(str2198d1(sz:8) (s: "def") )(dl12198dd(u:0)(l:2198b9)(r:219909))
```
(b)

Figure 23: Example Input and Output for Debug Print

2.5. Copying

The objective of making a copy of an instance of an ADT is essentially the same as that of the assignment operator in most programming languages, i.e., to make a copy of the object so that the original can be modified without changing the copy. For scalar ADTs the copy routines are simple, as shown in Figures 24 and 25 for an adt int and adt string, respectively. Note the seemingly unnecessary appearance of an "extra" input parameter named parent. In fact, this parameter is not used in these two copy routines, because there is no parent field to be set. However, in more complex ADTs, there may be a parent field that has to be set when a newly created instance is being copied into its new context. In this case the parent input parameter is necessary. The reason that the parent parameter is present here where it is not needed is because all required system-backbone routines must have exactly the same calling protocol. In other words, every copy routine must have exactly two input parameters, of which the parent is first and the object to be copied is second. The COPY macro also takes exactly these two parameters. Without this kind of uniform calling convention, it is impossible to develop a recursive mechanism for handling all the different classes of ADTs.

The code for copying an aggregate ADT uses the same recursive concepts as present in the rest of the system. The code for copying an adt pair is shown in Figure 26. Notice the continued use of the first parameter, which in this case is called dummy, since it is known that the incoming value will not be used.

 \mathbf{I}

```
INT TYPE
int_copy(parent, in)
       MEM TYPE
                      parent;
       INT TYPE
                      in;
\left\{ \right.INT TYPE
                      out;if (in == INT_NULL) RERROR(ABORT CODE, ("NULL pointer"));
       out = (INT_TYPE) mem man fixedsize allocate (int tag);
       INT_VAL(out) = INT_VAL(in);return (out);
\pmb{\}Figure 24: Copying an Instance of adt int
STRING TYPE
string_copy(parent, in)
       MEM TYPE
                            parent;
       STRING TYPE
                            in;
\mathbf{f}STRING TYPE
                            out:if (in == STNG NULL) RERROR(ABORT CODE, ("NULL position = "SING NULL) RERROR(ABORT CODE, ("NULL position = "SING NULL));
       out=(STRING_TYPE)mem man varsize allocate(string tag, STNG SIZE(in));
       STNG_SIZE(out) = STNG SIZE(in);
       strcpy(STNG_VAL(out), STNG_VAL(in));
       return (out);
\, }
                        Figure 25: Copying an Instance of adt string
PAIR TYPE
pair_copy(dummy, pair_in)
    MEM TYPE
                 dummy;
    PAIR TYPE
                  pair in;
\{PAIR TYPE
                  pair out;
    if (pair_in == PAIR_NULL) RERROR(ABORT CODE, ("NULL pointer"));
    pair_out = pair_create(COPY(MEM_NULL, LEFT_ELEMENT(pair_in)),
                      COPY (MEM_NULL, RIGHT_ELEMENT (pair_in)));
    return(pair out);
```
Figure 25: Copying an Instance of adt pair

The copy routine for a more complex aggregate ADT, an adt_dll, is shown in Figure 26. Note that here the parent parameter is used, because there is a parent field present in the ADT itself. It should now be clear why the uniform calling protocol for all copy routines is necessary. Also note the recursive

ADTs

```
DLL TYPE
dll_copy(parent, dll_in)
    MEM TYPE
                parent;
    DLL TYPE
                 dll in;
\mathfrak{f}DLL TYPE
                     dll out;
    LIST NODE TYPE \ln \bar{1}n;
    LIST NODE TYPE ln out;
    if (dll in == DLL NULL) RERROR(ABORT CODE, ("NULL pointer"));
    dll out = dll create (MEM NULL);
    PARENT (dll out) = parent;
    ln in = RIGHT(dll in);while (!DLL_IS_HEAD(ln_in)) {
        In out = list node copy ((MEM TYPE) dll out, \ln in);
        list node insert node to right ((MEM TYPE) dll out,
             LEFT(dll out), ln out);
        ln in = RIGHT(ln in);\mathbf{E}return(dll out);
}
```
Figure 26: Copying an Instance of adt dll

call to list_node_copy as the objects of the original input adt_dll are scanned and copied.

2.6. Comparing

For each ADT, a compare function must be supplied. This compare function is required to take two instances of the same ADT class and determine whether the first is less than, equal to, or greater than the second. Note that the creator of the new ADT class need only produce the compare function for two instances of the new ADT class being created. There is a macro, COMPARE, with extended logic which takes two instances of ADTs (from potentially different ADT classes) and determines their order. This COMPARE macro constitutes the computation of a total order of all instances of all ADT classes that reside in the system. Its logic will be presented in the discussion of aggregate ADTs.

The compare function for the ADTs can be used in a number of ways. The COMPARE macro is actually used internally in the implementation of some of the ADTs themselves. For instance the current implementation of adt set uses the COMPARE macro to essentially sort the objects that are in the instance of an adt set. Also, it is sometimes useful to sort objects to facilitate subsequent processing; but the criteria for the sort is unimportant. The generic COMPARE function, since it computes a total order on all instances of ADTs, can be used in such a generic sort.

The compare functions for adt int and adt string are given in Figures 27 and 28, respectively. Here, the type COMPARE TYPE is an enum containing three values: less than code, equal_code, and greater_than_code. The routine system_int_compare takes a single integer value as input and returns: less than code if the integer is less than 0, equal code if the integer is equal to 0, and greater_than_code if the integer is greater than 0. In this situation, a specific ordering of the instances of ADTs is specified by the code shown. For instance, for adt_int less_than code is returned if the first parameter is less than the second parameter. However, the code can be changed to reflect the reverse ordering and the system will still operate as desired. The total ordering of all instances of ADTs is preserved as long as each separate compare function maintains a total

```
COMPARE TYPE
int_compare(pl,p2)
      INT TYPE
                   p1;INT TYPE
                   p2;\mathfrak{g}COMPARE TYPE
                         ans;
      if (p1 == INT NULL) RERROR(ABORT CODE, ("NULL pointer"));
      if (p2 == INT NULL) RERROR(ABORT CODE, ("NULL pointer"));
      ans = system_int_compare(INT VAL(p1) - INT VAL(p2));
      return (ans);
```
 \mathbf{I}

Figure 27: Comparing Instances of adt_int

```
COMPARE TYPE
string compare(pl,p2)
      STRING TYPE pl, p2;
\mathfrak{t}COMPARE TYPE
                          ans:
      if (p1 == STNG NULL) RERROR(ABORT CODE, ("NULL pointer"));
      if (p2 == STNG NULL) RERROR (ABORT CODE, ("NULL pointer"));
      ans = system_int_compare(strcmp(STNG_VAL(p1), STNG_VAL(p2)));
      return (ans);\mathbf{I}
```
Figure 28: Comparing Instances of adt string

ordering within its single ADT class.

As a simple example of how to write a compare function for an aggregate ADT, consider the function pair compare shown in Figure 29. Here, the compare is biased toward the first component of the 2-tuple. If the first component of the first parameter is less than the first component of the second parameter, then the first parameter is declared to be less than the second parameter. Similarly, if the first component of the first parameter is greater than the first component of the second parameter, then the first parameter is declared to be greater than the second parameter. However, if the first component of each of the parameters is equal, then the second component must be interrogated to resolve the apparent tie. If the second component of the first parameter is less than the second component of the second parameter, then the first parameter is declared to be less than the second parameter. Similarly, if the second component of the first parameter is greater than the second component of the second parameter, then the first parameter is declared to be greater than the second parameter. However, if the second component of each of the parameters is equal, then the two parameters must be equal, because both of their components are equal.

Note the use of the macro COMPARE, which allows comparisons between instances of objects from different ADT classes. COMPARE works in the following simple way. Each ADT class has a unique tag associated with it. COMPARE compares the tags of the two instances of ADTs which are its input parameters. If the tags are different, the instance with the numerically smaller tag is declared to be less than the instance with the larger tag. If the tags are identical, then the instances are from the same ADT class, and the appropriate (unique) compare function is "looked up" and invoked to compare the two instances.

```
COMPARE TYPE
pair_compare(pairl, pair2)
    PAIR TYPE
                pairl;
    PAIR TYPE
                 pair2;
\{COMPARE TYPE
                         ans;
    if (pairl == PAIR_NULL) RERROR(ABORT CODE, ("NULL pointer"));
    if (pair2 == PAIR NULL) RERROR(ABORT CODE, ("NULL pointer"));
    ans = COMPARE (LEFT ELEMENT (pair1), LEFT ELEMENT (pair2));
    if (ans == equal code)ans = COMPARE(RIGHT ELEMENT(pair1), RIGHT_ELEMENT(pair2));return(an);
\mathcal{F}
```
Figure 29: Comparing Instances of adt pair

The compare function for an adt_dll is a bit more complicated, but retains the same idea as that used for the adt pair. It is shown in Figure 30. Here, the logic has one more level of complexity. In this case, first the cardinalities of the two lists are compared. If the cardinalities are different, then the one with the smaller cardinality is declared to be less than the one with the larger cardinality. If the cardinalities are identical, then the next level of test is applied. The corresponding objects in the two lists are compared starting at the beginning of each list. If the first objects in the two lists are not equal, then the declared

```
COMPARE TYPE
dll compare(dll1,dll2)
    DLL TYPE
                dlll;DLL TYPE
                 dll2;\mathbf{f}LIST NODE TYPE
                    ln 1;LIST NODE TYPE ln2;
    COMPARE TYPE
                         ans;
    if (dll1 == DLL NULL) RERROR(ABORT CODE, ("NULL pointer"));
    if (dl12 == DLL NULL) RERROR(ABORT CODE, ("NULL pointer"));
    ans = system int compare (dll cardinality (dll1) - dll cardinality (dl12));
    if (ans == equal code) {
        ln1 = RIGHT (dlll1);ln2 = RIGHT(dll2);while ((ans == equal code) && !DLL IS HEAD(ln1)) {
            ans = COMPARE(ln1, ln2);
            ln 1 = RIGHT(ln1);ln2 = RIGHT(ln2);\};
    \} ;
    return(ans);
\mathbf{I}
```


order of the two lists is determined by the order of the first two objects. If the first objects in the two lists are equal, then attention is focused on the second objects in the two lists. The order of the two lists is determined by discovering the first set of corresponding objects in the two lists which are not equal. If all the corresponding objects in the list turn out to be equal, then the two lists themselves are declared to be equal.

3. Object-operation Access Functions

The access functions presented so far constitute the required system-backbone access function which must be supplied for every ADT class. These access functions are used for managing the objects, but have nothing to do with the operations on the abstract data types for which they were created in the first place. For instance, a stack ADT might have a push operation and a pop operation associated with it.

Once the basic ADT class has been created and the system-backbone access functions produced, the creator of the ADT can supply any number of object-operations on the ADT desired. For example, for the adt int, the four basic arithmetic functions are shown in Figure 31. Obviously, more such access functions can be added for other arithmetic operations, such as mod and exp.

The concatenation function is shown for adt string in Figure 32.

Three object-operation access function that might be useful for adt pair are shown in Figure 33.

4. Management of ADTs

This section discusses how ADTs are managed within the DNA Mapping system. This includes how ADT classes are declared to the system, how the system maintains statistics about ADT instance utilization and reports this to the user, and how internal memory management is performed.

4.1. Declaring an ADT Class

Each ADT class used within the system must be declared to the system at execution time, usually done at initialization of the entire DNA Mapping system. This is done by invoking a number of routines associated with the memory management subsystem. Consider the declaration of adt int, as shown in Figure 34. The first executable statement simply insures that initialization is done no more than once. The three routines used to declare the properties of an ADT class are: mem_man_declare, mem man_set_destroy function, and mem_man_set_copy_function.

The first argument to mem man declare simply supplies a character string name for identification purposes during printing of tables. The second argument is an output parameter through which the system-created tag for the specific ADT class is returned. The third argument specifies the size of (i.e., the number of bytes of memory required) an instance of the ADT. If the ADT class is of fixed-size for all instances, then a positive integer is input; if the ADT class has variable-size instances, then a special code is used for this argument to indicate that it is of variable length. The next two arguments supply a pointer to the debug print and pretty print routines. The next two arguments supply a pointer to the create and compare routines. The last argument specifies the encodement used for the null pointer for the specific ADT class. Currently, all of these null pointers are encoded as 0.

The mem man set destroy function sets the destroy function for the specific ADT class. The mem man set copy function sets the copy function for the specific ADT class.

```
INT TYPE
 int\_add(p1, p2)INT TYPE
                          p1;INT_TYPE
                          p2;
 \left\{ \right.INT TYPE
                          ans;
         if (pl == INT_NULL) RERROR(ABORT_CODE, ("NULL pointer"));
         if (p2 == INT_{NULL}) RERROR(ABORT_CODE, ("NULL pointer"));
         ans = int_c \cref{INT_VAL(p1)} + INT_VAL(p2));return(ans);
\boldsymbol{\mathcal{Y}}INT TYPE
int\_sub(p1, p2)INT_TYPEp1;INT TYPE
                          p2;
         INT TYPE
                         ans;
         if (pl == INT_MULL) RERROR(ABORT CODE, ("NULL pointer"));
         if (p2 == INT NULL) RERROR (ABORT CODE, ("NULL pointer"));
         ans = int_c \text{create}(\text{INT}_VAL(p1) - \text{INT}_VAL(p2));return (ans);\mathcal{Y}INT TYPE
int_mult(p1, p2)INT TYPE
                         p1;INT_TYPE
                         p2;\mathbf{f}INT TYPE
                         ans;
        if (pl == INT_NULL) RERROR(ABORT CODE, ("NULL pointer"));
        if (p2 == INT_NULL) RERROR(ABORT CODE, ("NULL pointer"));
        ans = int\_create(INT\_VAL(p1) * INT\_VAL(p2));return (ans);
\, \,\texttt{INT\_TYPE}int_div(p1,p2)
        INT_TYPE
                         pl;
        INT TYPE
                         p2:\{INT TYPE
                         ans;
        int.
                          i1;int.
                          i2;
        if (p1 == INT_NULL) RERROR(ABORT CODE, ("NULL pointer"));
        if (p2 == INT NULL) RERROR(ABORT CODE, ("NULL pointer"));
        i1 = INT_VAL(p1);i2 = INT_VAL(p2);if (i2 == 0) RERROR (ABORT CODE, ("Attempt to divide by zero"));
        ans = int create(i1/i2);
        return(ans);
\pmb{\}}
```
Figure 31: Arithmetic functions for adt int

```
STRING_TYPE
string concat (s1, s2)
    STRING TYPE sl:
    STRING_TYPE s2;
\{STRING TYPE
                   \mathbf{p};
    int
                       size;
      if (s1 == STRING_NULL) RERROR(ABORT CODE, ("NULL pointer"));
      if (s2 == STRING_NULL) RERROR(ABORT CODE, ("NULL pointer"));
    size = sizeof(STR_NSTRING_TYPE)+ strlen(\overline{STNG\_VAL}(s1)) +strlen(\overline{STNG\_VAL}(s2)) +1;
    p = (STRING_TYPE) mem_man_varsize_allocate(string_tag,size);
    STNG_SIZE(p) = size;
    strcpy(STNG_VAL(p), STNG_VAL(s1));
    \texttt{strcat}(\texttt{STNG\_VAL}(p), \texttt{STNG\_VAL}(s2));return(p);\mathbf{E}
```
Figure 32: Concatenation for adt_string

ADTs

```
MEM TYPE
pair_get_left_element(pair)
    PAIR TYPE
                 pair;
\mathbf{I}ans;
    MEM TYPE
    if (pair == PAIR NULL) RERROR(ABORT CODE, ("NULL pointer"));
    ans = LET_ELEMENT(pair);return(ans);
\mathbf{I}void
pair set left element (pair, data)
    PAIR TYPE pair;
    MEM TYPE
                      data;
\{if (pair == PAIR_NULL) RERROR(ABORT_CODE, ("NULL pointer"));
    LEFT ELEMENT (pair) = data;
    util_set_destruction(&PAIR_LEFT_UTIL(pair), UTIL_CAN_DESTROY);
    return;
\mathbf{L}PAIR_TYPE
pair_create_by_swap(p)
    PAIR_TYPE p;
\mathfrak{f}PAIR TYPE newp;
    if (p == PAIR NULL) RERROR(ABORT CODE, ("NULL pointer"));
    newp = pair create ddd(pair get right element(p)),pair get left element (p) ) ;
    return (newp);
\mathcal{Y}
```
Figure 33: Object-operations for adt pair

```
void
int ds init ()
\{if (int_init_done) return;
      if (int_tag == NULL TAG) {
            mem_man_declare("int ds", &int tag, sizeof(STR INT TYPE),
                         int dprint, int pprint, (MFUNC TYPE)
                         int_create, int_compare, (NULL_TYPE) INT_NULL) ;
      \cdotmem_man_set_destroy_function(int tag, int destroy);
      mem_man_set_copy_function(int_tag,(MFUNC_TYPE)int_copy);
      int init done = TRUE;return;
\big\}
```
Figure 34: Declaration of adt int

The memory management system accepts all of these parameters and places them in a table, the entries of which will be used during the remainder of the execution. This table is implemented as an array of a struct. The structure of the struct is shown in Figure 35. All of the fields present in the actual DNA Mapping software are not present here; only those which are pertinent to the discussion at hand have been included. The first nine fields included in this struct have already been discussed in the previous few paragraphs. The remainder will be introduced in subsequent subsections.

The declaration for a variable-size ADT class is very similar, as shown in Figure 36 for adt string. Note that there is only one slight change to the scheme; the third argument to mem man declare is VAR SIZE DS CODE, which stands for "variable size data structure code". The value of this constant is -1, and indicates to the system that this is a variable-size ADT class.

The declarations for adt_pair and adt_dll are very similar, and are shown in Figures 37 and 38.

struct adt tab entry (
STRING	name fld;
int	size fld;
VFUNC TYPE	dprint fld;
VFUNC TYPE	pprint fld;
NULL TYPE	null pnt fld;
MFUNC TYPE	create fld;
VFUNC TYPE	destroy fld;
CFUNC TYPE	compare fld;
MFUNC TYPE	copy fld;
int	total_obj_fld;
int	max obj fld;
int	cur obj fld;
PNT AVAIL TAB ENTRY TYPE	avail tab fld;
ĩ	

Figure 35: Memory Management Table Structure

```
void
string_ds_init()
\{if (string_init_done) return;
       if (\text{string\_tag} == \text{NULL\_TAG}) {
             mem_man_declare("string_ds", & string_tag, VAR_SIZE_DS_CODE,
                           string dprint, string pprint,
                           (MFUNC_TYPE) string_create,
                           string compare,
                           (NULL TYPE) STRING NULL) ;
       \} :
       mem man set destroy function (string tag, string destroy);
      mem_man_set_copy_function(string_tag,(MFUNC_TYPE)string_copy);
       string\_init\_done = TRUE;return;
\mathbf{r}Figure 36: Declaration of adt_string
void
pair ds init ()
ſ
    if (pair_init done) return;
    if (pair_tag == NULL TAG) {
        mem man_declare("pair_ds", &pair_tag,
                  sizeof (STR PAIR TYPE),
                  pair_dprint, pair_pprint, pair_create,
                  pair compare, (NULL TYPE) PAIR NULL);
    \} ;
    mem_man_set_destroy_function(pair_tag,pair_destroy);
    mem_man_set_copy_function(pair_tag,(MFUNC_TYPE)pair_copy);
    pair\_init\_done = TRUE;return;
\mathbf{I}
```
Figure 37: Declaration of adt_pair

```
void
dll ds init ()
\{if (dll init done) return;
    if (dll tag == NULL TAG) {
        mem man declare ("dll ds", &dll tag, sizeof (STR DLL TYPE),
                 dll dprint, dll pprint, dll create,
                 dll compare, (NULL TYPE) DLL NULL);
    \mathbf{E}mem_man_set_destroy_function(dll tag,dll destroy);
    mem_man_set_copy_function(dll tag, (MFUNC TYPE)dll copy);
    list node ds init();
    dll init done = TRUE;
    return;
\mathcal{L}
```
Figure 38: Declaration of adt_dll

4.2. Statistics on Instances of ADTs

The user can print a table which presents statistics about the current status of the ADTs. An example of such a table is shown in Figure 39. The last column indicates the name of the ADT class as specified during its declaration; it is included as a reference to externally name the ADT class. The first column indicates how many instances of the specific ADT class are currently allocated. The value printed here is extracted from the cur obj fld field of the internal ADT table (cf. Figure 35). This field is incremented every time an instance of the specific ADT class is created and decremented every time an instance of the specific ADT class is destroyed. The second column indicates the maximum number of instances of the ADT class that have ever been allocated an one specific time; it is essentially a "high water mark" indicating how much of a resource bottleneck this particular ADT class represents. The value printed here is extracted from the max obj fld field of the internal ADT table (cf. Figure 35). This field is modified every time an instance of the specific ADT class is created to calculate the current maximum. The third column indicates how many instances of the specific ADT class have ever been allocated. The value printed here is extracted from the total obj fld field of the internal ADT table (cf. Figure 35). This field is incremented every time an instance of the specific ADT class is created; it is never decremented. The fourth column indicates the (user-specified) size, in bytes, of the memory required to hold an instance of the ADT. Notice that several ADT classes have a -1 in this column, indicating that they are variablesize ADTs. The fifth column indicates the actual tag used internally for the specific ADT class. In fact, this tag is a pointer (in memory) to the entry in the internal ADT table for this specific ADT class. In other words, the tag is actually a pointer to a record (i.e., struct) which contains all the functions needed to access a specific instance of the ADT class and all the data fields necessary to maintain running statistics about the ADT class as a whole.

Notice that there are a number of lines at the bottom of the table which refer to the amount of memory which has been allocated from the operating system. The first line indicates the total memory that has been allocated from the operating system. This includes more than just ADT memory; certain DNA Mapping system tables are dynamically allocated, but are not built by using ADTs. The second line indicates how much memory has been allocated for use by ADTs. Specifically, the DNA Mapping system does its own memory allocation and management. Large blocks of memory (by default set at a size of 1K) are allocated from the operating system, and memory for individual instances of ADTs is allocated from these blocks. No memory is ever returned to the operating system. The third line indicates how large a block will be allocated the next time a block of memory is needed from the operating system. The size of the block allocated from the operating system can be controlled by invocation of the function mem man numK. The fourth line indicates how much memory is currently available in the last block that was allocated. The last line indicates how much miscellaneous memory has been allocated. (Miscellaneous memory is a special class of memory which cannot be returned even internally to the DNA Mapping

Total memory allocated is 140248 bytes. Total ADT memory allocated is 137216 bytes. Current block allocation size is 1K bytes. 936 bytes in current block. 53 bytes of misc memory.

Figure 39: Statistics about ADTs and Memory Management

system.)

The data in this table can be used to determine the memory resources used in any specific computational activity. This table is extremely useful in the process of "zeroing out" memory. At the end of a computation, the "currently allocated" column of this table should be 0 for all ADT classes, except miscellaneous memory. If a particular entry is not 0, then instances of that ADT class are still allocated, and the application has failed to deallocate (destroy) unused objects. Great care must be taken to destroy all

instances of ADTs which are no longer useful. Failure to do so can cause memory exhaustion and cause execution of an otherwise correctly executing program to abort.

4.3. Memory Management

The DNA Mapping system does its own memory management internally. No calls to malloc, calloc, or realloc are present; thus, the use of free is not possible. Instead, all allocation of memory from the operating system is done through invocations to the system routine sbrk. (The application programmer should not use malloc or any of its variations, because sbrk and malloc are incompatible with each other.) Large blocks of memory (by default set at a size of 1K) are allocated from the operating system, and memory for individual instances of ADTs is allocated from these blocks. The size of the block allocated from the operating system can be controlled by invocation of the function mem man numK. No memory is ever returned to the operating system.

Memory nodes which are returned to the system for future use are stacked in avail lists for future reallocation. There is a separate avail list for each individual node size which has been returned to the system. An array of headers for these avail lists is maintained.

4.3.1. Allocation

As a request for a memory node of a specific size is processed, the system first checks to see if there is an avail list for this size node and whether there is a memory node currently available. If a memory node is available, it is extracted from the avail list and returned to whoever requested the memory. If there is no such node available in an appropriate avail list, the current memory block is checked to determine if there is enough memory left in the block to satisfy the request. If there is enough memory present, the correct amount is extracted from the current memory block and returned to whoever requested the memory. If there is not enough memory present in the current memory block, a new block of memory is allocated from the operating system and the required amount of memory is extracted from it. This is the basic logic as expressed in mem man get mem, as shown in Figure 40. Here, the two input parameters are (a) the tag of the object for which memory is being requested and (b) a pointer to an avail list header where memory nodes of exactly the correct size may be present.

The first executable statement computes the actual size of the memory needed, including the memory for the tag. The second statement, invoking avail get, attempts to allocate memory from the appropriate avail list. The rest of the code is applicable only if memory could not be extracted from the avail list. next memory is a pointer into the current memory block where the next (currently unallocated) available byte of memory will be found. Last memory is a pointer to the next byte after the current memory block. numK to sbrk is a global variable which indicates how much memory to allocate from the operating system; it can be modified by invoking mem man numK. The routine mem alloc invokes sbrk to get the next memory block from the operating system. The routine mem man cannot alloc reports memory exhaustion and offers the user several interactive options.

The routine mem man get mem is invoked by mem man fixedsize allocate and mem man varsize allocate as shown in Figures 41 and 42, respectively. In mem man fixedsize allocate the macro AVP FIELD extracts the appropriate avail list header from the internal ADT table. This is the last field, avail tab fld, of the struct shown in Figure 35. For fixed-size ADT classes, this field is initialized at declaration time to point to an avail list with appropriately sized memory nodes. This size is computed by adding the user-specified data structure size to the size of a tag.

Memory is allocated and a pointer to it resides in the variable ans. The value of the tag is inserted at the beginning of the memory, and the variable ans is incremented by the length of a tag so that ans now points to the user-specified portion of the memory which has been allocated. This is the value returned in the last executable statement. The three executable statements just prior to the return update the

ADTs

```
MEM TYPE
mem_man_get_mem(tag,av)
     TAG TYPE
                                      tag;
     PNT AVAIL TAB ENTRY TYPE
                                      av:\left\{ \right.int
                  size;
    MEM_TYPE
                 ans;
     int \frac{1}{2}mem_to_allocate;
     size = SIZE FIED(av);ans = \arctan\left(\frac{1}{2}gt\right) (av) ;
                                     /* try to get memory for avail list */
    if (ans == MEM NULL) { \frac{32}{7} to do block allocation \frac{1}{7}if ((next memory==MEM NULL)| | (next memory+size>last memory)) {
              mem to allocate = MAX (size, numK to sbrk*1024);if ((next_memory = mem_allloc(mem_to_allocate))!= MEM FAIL CODE) \overline{ }total adt mem += mem to allocate;
                       last memory = next memory + mem to allocate;
                       ans = next_memory;next_memory += size;\mathcal{F}else { }mem_man_cannot_alloc(tag);
              \} ;
         \mathcal{E}else (
              ans = next_meanory;next_memory += size;
         \} ;
    \mathcal{F}return(ans);
\mathcal{Y}
```
Figure 40: Code for mem man get mem

```
MEM TYPE
mem man fixedsize allocate (tag)
    TAG TYPE
              tag:
\{MEM TYPE
                     ans;
            /* get some memory */
    ans = mem_man_get_mem(tag, AVP_FIELD(tag));
            /* insert the tag and increment to user portion */* ((PNT_TAG_TYPE) ans) ++ = tag;
            /* increment # of nodes allocated */CURO FIELD (taq) + fTOTALO FIELD (taq) ++;
            /* calculate max */MAXO FIELD (tag) = MAX (CURO FIELD (tag), MAXO FIELD (tag));
    return(ans);
\mathbf{1}
```
Figure 41: Code for mem man fixedsize allocate

appropriate statistics about (a) the current number of instances allocated, (b) the total number of instance allocated, and (c) the maximum number of instances allocated.

The code for mem_man_varsize_allocate is very similar. There are only two differences. First, the (user-specified) size is specified as an input parameter. Second, in the call to mem man get mem, the appropriate avail list header must be computed. This cannot be preprocessed at declaration time, as with a fixed-size ADT class, because the size of each instance cannot be known at declaration time. The macro ACT SIZE (i.e., actual size) takes its input parameter and adds the size of a tag. The routine avail tab lookup searches the array of avail list headers for one corresponding to memory nodes of the appropriate size; if none is present, one is inserted. The rest of the code is identical to

```
MEM TYPE
mem man varsize allocate (tag, size)
    TAG TYPE taq;
    int
                  size;
\overline{\mathfrak{l}}PNT ADT TAB ENTRY TYPE
                               \mathbf{D}:
    MEM TYPE
                      ans;
             /* get some memory */ans = mem man get mem(tag, avail tab lookup (ACT SIZE (size)));
             /* insert the tag and increment to user portion */* ((PNT TAG TYPE) ans) ++ = tag;
             /* increment # of nodes allocated */CURO FIELD (taq) + +;
    TOTALO FIELD (tag) ++;
             /* calculate max */MAXO FIELD (tag) = MAX (CURO FIELD (tag), MAXO FIELD (tag));
    return(an);
\mathbf{1}
```
mem man fixedsize allocate.

4.3.2. Deallocation

As instances of ADTs are destroyed, their memory is deallocated or returned by calling one of two routines: mem man fixedsize deallocate and mem man varsize deallocate. The code for mem_man_fixedsize_deallocate is shown in Figure 43. The logic for this routine is somewhat complicated by the fact that instances of both fixed-size and variable-size ADTs can be returned through the use of this routine. (Recall that the convention for variable-size ADTs is to make the first field of the user-specified data structure a field which hold the size of the memory which was allocated.) The TAG OF macro "looks up" the tag of the instance of the ADT which was input, node. (Once the tag is known, the size of the ADT can be determined. If the size is greater than zero, the ADT is a fixed-size ADT; if the size is -1, the ADT is a variable-size ADT.) The SIZE FIELD macro extracts the field size fld from the internal ADT table (cf. Figure 35) to determine whether it is a fixed-size ADT or a variable-size ADT. If size is greater than 0 (i.e., a fixed-size ADT), then the macro AVP FIELD extracts the appropriate avail list header which was determined during the declaration of the ADT class. Otherwise this is a variable-size ADT and the appropriate avail list header must be computed. The SIZE OF macro looks in the first word of the (user-specified) data structure to extract the size of the memory present. To this, the macro ACT SIZE adds the size of the tag, and the routine avail_tab_lookup searches the array of avail list headers for the one which corresponds to the appropriate size; a header is inserted if one of appropriate size is not present. Some statistics bookkeeping is done. The variable node which originally pointed to the user-specified portion of the data structure is decremented to point to the tag which occurs just to the left. This memory pointer is then inserted into the appropriate avail list, as specified by the avail list header which was previously computed.

The logic of mem man varsize deallocate, as shown in Figure 44, is much simpler. Here, the tag is "looked up", and the appropriate statistics bookkeeping is done. The correct avail list header is computed, and the memory is inserted into the appropriate avail list for potential future use.

```
void
mem man_fixedsize deallocate(node)
    MEM TYPE
                 node;
ŧ
    TAG TYPE
                                   tag;
    PNT AVAIL TAB ENTRY TYPE
                                   av1;int
                                   size;
    tag = TAG OF(node);\sqrt{\ast} determine size and check \sqrt{\ast}size = SIZE FIELD (tag);
    if (size > 0) avl = AVP FIELD(tag);
    else avl = avail tab lookup (ACT SIZE (SIZE OF (node)));
             /* decrement # of allocated nodes \bar{x}/CURO FIELD (tag) --;/* move back to beginning of memory */-- ((PNT TAG TYPE) node);
             /* put memory on avail list */avail put (avl, node);
    return;
\mathbf{r}
```

```
void
mem man varsize deallocate (node, size)
    MEM TYPE
               node;
    int
           size:
\{TAG TYPE
                     tag;
    PNT_ADT_TAB_ENTRY_TYPE p;
    tag = TAG OF(node);/* decrement # of allocated nodes */
    CURO FIELD (tag) --;/* move back to beginning of memory */
    -- ((PNT_TAG_TYPE)node);
            /* put memory on avail list */
    avail put (avail tab lookup (ACT SIZE (size)), node);
    return;
\mathbf{I}
```
Figure 44: Code for mem man varsize deallocate

5. System ADTs

At this point, only four ADTs have been discussed in detail: adt int, adt string, adt pair, and adt dll. (adt list node also has been mentioned in passing.) In this section, a number of other ADT classes present in the DNA Mapping system are discussed briefly. No code is presented, and only basic ideas and intent are discussed. The ADT classes are subdivided into three categories: (a) very general ADTs that might be included in almost any application, (b) general ADTs of a less universal nature, and (c) ADTs specific to the DNA Mapping project itself.

5.1. General Purpose ADTs

In this section, a number of generic ADTs that might occur in almost any application are presented briefly.

Two standard scalar data types are Boolean and float. There are two ADTs, adt bool and adt float, which encapsulate these scalars. It should be obvious what their intent is, and they will not be discussed further.

A very important generic ADT is adt list which is an extension of adt dll. In fact, adt list is built on top of adt dll (i.e., uses adt dll as a component in its implementation). adt list implements an aggregate which can be thought of dually (i.e., concurrently) as either a linked list or an array. For instance, it is possible to ask for the 9th object in the list, or to request that an object be inserted after the 9th object in the list. Of course, it still is possible to extract and insert data at either end of the list. adt list also has one other important new feature, the concept of a current position. This gives adt list the property of having a state. For instance, it is possible to place the current pointer at the beginning of a list and incrementally "march through" the list by advancing the current pointer. There are many access functions available for adt list, such as concatenation of lists, sorting of a list, reversing a list, etc. There are currently more than 100 access functions and 50 access macros defined on adt list.

adt set is another interesting ADT. It implements the abstract mathematical concept of a set, in which no duplicates are allowed, adt set is built on top of adt list. In order to make operations such as union, intersection, and membership efficient, the elements of a set are sorted (inside an adt list) so that searching and merging can be done efficiently. Here, the macro COMPARE is used to determine the order of the ADT instances.

The concept of a stack is achieved through the introduction of adt stk. This also is built on top of adt list. The standard operations of push, pop, empty, etc. are supplied as object-operations.

The concept of an array of ADTs is achieved through the introduction of adt marray (i.e., memory array). In this ADT any finite length array can be allocated with user-specified upper and lower index bounds. In this implementation random access to an arbitrary index position is achieved in constant time (as in a random access array), whereas the array indexing feature of adt list requires "marching through" the elements of a linked list to find the correct index position.

The concept of a bit vector is achieved through the introduction of adt bity. In this ADT any finite length bit vector (i.e., array of Boolean) can be allocated with user-specified upper and lower index bounds. This is useful for implementing the simulation of sets for which the members are known a priori. For instance, the adjacency matrix of an arbitrary graph easily can be implemented by construction an adt marray of adt bitvs.

The concept of a hash table is achieved through the introduction of adt hashtab. This is implemented on top of adt array. This ADT supplies the standard operations of inserting data based on a key and then subsequently searching for the data which is associated with a specific key.

5.2. Other General ADTs

In this section ADTs of general interest, but of a less general nature are introduced. Here, only the general concept associated with the ADT is presented.

There are a number of ADTs which address the mathematical formalism of a graph. Specifically, adt digraph simulates the realization of a directed graph. Similarly, adt bigraph simulates the realization of a bipartite graph. Both of these are built on top of two other ADTs, adt edge and adt vertex.

Another mathematical abstraction is achieved through adt bag. The mathematical concept of a bag is similar to that of a set, except that the same object can occur more than once in a bag whereas an object can occur no more than once in a set.

Two operations associated with graphics have been implemented, adt point implements the concept of a point in Cartesian coordinates, i.e., a 2-tuple of floats. adt line implements the concept of a line segment, i.e., a 2-tuple of adt points.

Three ADTs have been implemented to simulate combinatorial concepts. Specifically, adt perm implements the concept of permutations. In other words, given a set of objects (instances of ADTs), adt_perm will produce, one at a time, every permutation possible for that set of objects. Similarly, adt combo implements the concept of combinations. In other words, given a set of objects, adt combo will produce, one at a time, every combination possible (of a given size) for that set of objects. adt odometer simulates the idea of a generalized odometer (as in the odometer of a car). It is given a list of lists of objects. Each element of the top-level list (which is a list itself) corresponds to a wheel of the odometer. The objects in each secondary list correspond to the "characters" that reside on the wheel. adt odometer returns, one at a time, a list of objects corresponding to what would appear on the concatenation of the wheels as the least significant wheel continues to turn, recursively causing subsequent wheels to turn.

An interesting form of a list has been introduced through the inclusion of adt rlist (i.e., reversible list). The general implementation of a list, as expressed through adt list, gives all of the functionality needed for manipulating lists, including concatenation of lists and reversal of a list. However, within its implementation the operations of concatenation and reversal are not of $O(1)$ time complexity. It was not possible to modify the implementation of adt_list to make these operations of O(1) time complexity and

still retain the generality that had been built into adt list, for which there are a large number of access functions. adt rlist was created to supply a restricted form of a list in which both the concatenation function and the reversal function are of $O(1)$ time complexity.

5.3. DNA Mapping ADTs

There also are several ADTs which are directly related to DNA Mapping concepts. For instance, adt rfrag implements the concept of what is referred to as a real fragment. A real fragment corresponds to an actual fragment present in a clone as identified through the process of electrophoresis. The term "real fragment" is meant to imply that the fragment is known to exist (via visual inspection of the electrophoresis gel). A real fragment has: (a) a name, (b) a measured length, and (c) estimates as to the right and left error bounds on the measured length.

In contrast, adt vfrag implements the concept of what is referred to as a virtual fragment. A virtual fragment corresponds to a fragment present in a map unit. A virtual fragment is derived from one or more real fragments which have been inferred to come from the identical region of a genome. However this inference is a working hypothesis, and the virtual fragment (as derived from its constituent real fragments) may not exist at all. The length of a virtual fragment is the average of the lengths of the real fragments which constitute it.

Several forms of tree are implemented by adt tree. The most important form of tree is the sequence-set tree (SST). SSTs are used to encode the group/fragment information present in a map unit. Specifically, in a map unit there is a sequence of groups, each group containing one or more fragments. The order of the groups is known (i.e., sequence), but the order of the fragments within each group is not known (i.e., set). For instance, the SST shown in Figure 45 corresponds to the map unit shown in Figure 46.

In performing DNA mapping and attempting to map a clone into a map unit, a window of interest (just slightly larger than the clone) is "dragged" across the map unit at group boundaries. At each window position, an attempt is made to map the clone within the portion of the map unit defined by the window. Since the concept of a map unit is encoded as an SST, a windowing mechanism is needed for defining a contiguous subregion of the tree. adt window supplies this physical mechanism. Within an instance of

Figure 45: A Sequence-set Tree

Figure 46: A Map Unit

adt_window two pointers identify two set nodes within an SST. The groups corresponding to the set nodes (inclusively) between these two pointers define the window in the map unit.

5.4. Pseudo ADTs

Besides the formal ADTs that have been discussed, there are a number of pseudo ADTs that have been produced. They are referred to as pseudo ADTs because the do not formally have a distinct tag associated with them, but instead are built from a combination of other formal ADTs. Four of the current pseudo ADTs are function, mu, partition, and relation. function implements the mathematical concept of a function. In other words, a set (i.e., adt set) of 2-tuples (i.e., adt pair) in which the set of values occurring in the first component must be unique with respect to the second component. mu implements a number of useful functions on map units, expressed as sequence-set trees (SSTs). (The reason that this is separated from the implementation of SSTs is that SSTs are an abstraction which can have trees of any height or mixture of node types, whereas map units have exactly three tiers of rigidly structured nodes.) partition implements the concept of a partition of a set. relation implements the mathematical concept of a relation, i.e., a set of 2-tuples for which there is no restriction on the uniqueness of the components.

6. Conclusions

The use of the ADTs described in this report has made it possible to quickly create prototypes of many of the DNA Mapping algorithms. The self-identifying nature of the execution-time tagged architecture combined with the required system-backbone access functions produce a framework in which it is possible to create, copy, compare, print, and destroy data structures of unbounded complexity. Their utility stems from their object-oriented nature, making it possible to construct arbitrarily complex aggregates of data structures without the intellectual or physical effort normally required to understand and implement the details at each level of the aggregation.

The aggregate nature of many of the general purpose ADTs makes it possible to create a data "bridge" between different computational components of a complex algorithm. The aggregate output of one routine (say a list of objects) can be made available as the input to any number of routines for subsequent processing. The aggregate can be passes through routines and be perceived as a single object until it is necessary to unbundle the collection to extract its parts for individual processing. The concept is very similar to that of a pipe in the UNIX operating system. In the case of a pipe, UNIX uses a file (either on disk or in memory) to communicate information between processes. This file is an aggregate of information, the syntax of which both the creator and the receiver must understand. The receiver can choose to pass on the information to a subsequent process without any modifications, or it can choose to "filter" the information passed through it in any number of ways. The aggregate ADTs supply a similar encapsulation mechanism between computational components of an application, using well-known concepts and structures. In a similar manner that the concept and use of a pipe encourages modularity and communication, the ADT paradigm enhances the ability to modularize and parameterize the implementation of an application. This modularity allows algorithms to be reconfigured quickly into variations of the original algorithm.

Once the basic idea behind ADTs is understood, it is not difficult to design and implement new ADT classes. It often is appropriate to use already implemented ADTs as constituent components of a new ADT being created. For instance, in the current ADTs implemented within the DNA Mapping system, adt dll is built on top of adt list node, adt list is built on top of adt dll, and adt set is built on top of adt list. Many other ADTs are interdependent also.

Since the ADT classes are declared at execution time, the entire system need not be recompiled as a new ADT class is introduced. No compile-time tables keep track of what ADTs are or are not present; thus, no compile-time objects have to be changed to reflect the introduction of a new ADT. The creator of a new ADT class need only program the required system-backbone and object-operation access function and include the declaration of the new ADT within the initialization activities of the system.

Although the use of ADTs supplies a very flexible and powerful framework for the application programmer, it also forces significant responsibility onto the application programmer. The programmer must be careful not to produce "circular" data structures whose recursive nature will confuse the simple-minded aggregate ADT management framework. The programmer must also be vigilant to destroy all instances of ADTs which are no longer needed. This requirement often dictates the style and structure of the algorithms produced. This can be thought of as either an advantage or a disadvantage. It has been found that the discipline imposed by "memory zeroing" restrictions often produces algorithms of much better structure than would have been produced if the restrictions were not present. This tends to make the resulting algorithms more modular, modifiable, verifiable, and reconfigurable.