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## Flexible Maximum Urgency First Scheduling for Distributed Real-Time Systems

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In the rest of this report, we first describe the design of the FMUF scheduling strategy. Then, we present simulation results to demonstrate that FMUF can provide performance isolation for mission-critical tasks.

## 2 FMUF Scheduling

The following are some definitions for *FMUF* Scheduling strategy:

-Two types of tasks: *mission-critical* tasks and *best effort* tasks, categorized by its importance specified by users.

-All real-time priorities are divided into two classes: a high priority class and a low priority class. A task whose priority is in the high priority class is in the *high* group. The other tasks are in the *low* group. That is, a task in the *high* group always has a higher priority than any tasks in the *low* group. *Inside* each group, all tasks are ordered by their end-to-end deadline, and end-to-end Deadline Monotonic scheduling algorithm is applied to assign subpriorities.

The basic idea of FMUF is to utilize an adaptive mechanism to dynamically adjust the priority of *best effort* tasks (i.e., move some best effort tasks into or out of the *high* group) according to the current conditions at runtime. In the rest of this section, we present two approaches to implement this strategy.

### 2.1 End-to-end Task Model

A system has  $m$  end-to-end periodic tasks  $\{T_i | 1 \leq i \leq m\}$  executing on  $n$  processors  $\{P_i | 1 \leq i \leq n\}$ . Task  $T_i$  is composed of a chain of subtasks  $\{T_{ij} | 1 \leq j \leq n_i\}$  that may be allocated to multiple processors. A subtask  $T_{ij} (1 \leq j \leq n_i)$  cannot be released for execution until its predecessor  $T_{i,j-1}$  is completed. a non-greedy synchronization protocol (e.g., release guard [1]) is used to enforce the precedence constraints between subsequent subtasks. Hence, each subtask  $T_{ij}$  of a periodic task  $T_i$  is also periodic and shares the same rate as  $T_i$ . Each task  $T_i$  is subject to an end-to-end relative deadline related to its period.

### 2.2 FMUF based on deadline miss ratio

In this approach the priorities of some *best effort* tasks are adjusted based on the history of deadline miss. We first introduce several notations:

- $T_0$ : the *best effort* task whose priority has just been adjusted in the latest adaptation operation
- $U_{i,k}$ : the total utilization of processor  $P_i$  during the  $k^{th}$  sampling period
- $S_i$ : the set of processors that host subtasks of  $T_i$

*The Logic of FMUF*

1. At the start time of the system, place all *mission-critical* tasks into the *high* group (by assigning high priority to them); and add all *best effort* tasks into the *low* group (by assigning low priority to them); set  $T_0 = null$

2. In the end of every sampling period, monitor the total utilizations  $\{U_{i,k} | 1 \leq i \leq n\}$  of all processors and check the deadline miss of all tasks
  - (a) **If** there is deadline miss in the *high* group, move a best effort task  $T_s$  from the *high* group to the *low* group (by decreasing its priority), and set  $T_0 = T_s$
  - (b) **If** (i) there is no deadline miss in the *high* group for consecutive  $N$  ( $N > 1$ ) sampling periods and (ii) there are deadline misses in the *low* group, choose one best effort task  $T_s$  from the *low* group according to some selection policies (e.g., shortest end-to-end deadline first)
    - i. **If**  $T_s \neq T_0$ , **then** move  $T_s$  to the high group (by increasing its priority), and set  $T_0 = T_s$
    - ii. **Else** calculate  $\Delta U_i = U_{i,k-1} - U_{i,k}$  for all processors in  $S_s$ ; if  $\min_{P_i \in S_s} \Delta U_i \geq threshold$ , then move  $T_s$  to the high group

In this approach, an adaptation operation can be triggered by several reasons, such as the arrival and departure of mission-critical tasks, and significant variation of execution times. The *threshold* is defined to avoid oscillation of the system, i.e., one task has been moved into and out of the high group repeatedly. The value of *threshold* need to be tuned.

Here is one simple example to demonstrate how FMUF works. In this example, we set  $N = 5$  and *threshold* = 5%. The workload includes 7 tasks: three *mission-critical* tasks,  $T_1$  with end-to-end deadline  $D_1 = 400$ ,  $T_2$  with  $D_2 = 500$ , and  $T_3$  with  $D_3 = 600$ ; four *best effort* tasks,  $T_4$  with  $D_4 = 350$ ,  $T_5$  with  $D_5 = 300$ ,  $T_6$  with  $D_6 = 400$ , and  $T_7$  with  $D_7 = 550$ . There are two processors. Each task has one subtask on each processor. In the beginning of the  $(k-1)^{th}$  sampling period, there is no deadline miss for all tasks. All three *mission-critical* tasks are in the *high* group, whereas there are two *best effort* tasks,  $T_4$  and  $T_5$ , in the *high* group. Other two *best effort* tasks are in the *low* group. During the  $(k-1)^{th}$  sampling period, execution time of  $T_1$  increases significantly, which incurs  $T_3$  miss deadline. An adaptation operation is triggered at the end of  $(k-1)^{th}$  sampling period. The best effort task with the longest end-to-end deadline in the *high* group,  $T_4$  here, is moved to the *low* group.  $T_0$  is set to  $T_4$ . For the next 10 sampling periods, there is no deadline miss in the *high* group while deadline miss occurs in the *low* group. Adaptation operation is triggered in the end of each sampling period. However, as  $T_s$  is always equal to  $T_0$  and the utilization deviations of two processors are both less than the *threshold* 5%, no task will be moved to the *high* group according to the algorithm. At the end of  $(k+10)^{th}$  sampling period,  $T_2$  departs from the system. The utilization of either  $T_{21}$  or  $T_{22}$  is greater than 5%. Then after the adaptation operation,  $T_4$  will be moved back to the *high* group. In this example, we select the *best effort* task to adjust priority according to the end-to-end deadline in order to decrease the priority inversion. We can easily replace this with other selection policies.

### 2.3 FMUF based on AUB condition

In this algorithm, we try to adjust the priority of some *best effort* tasks based on Aperiodic Utilization Bound (AUB) for end-to-end tasks [2]. We use AUB

to guarantee all tasks in *high* group meet their deadlines. The schedulability condition of Aperiodic Utilization Bound is computed by:

$$\sum_{j=1}^N \frac{U_j(1 - U_j/2)}{1 - U_j} \leq 1 \quad (1)$$

$N$  is the number of processors;  $U_j$  is the estimated utilization of subtasks in *high* group on processor  $j$ ,  $U_j = \sum_{T_i \in G_j} C_{ij}/D_i$ . For simplicity, in the rest of this section, we call inequation 1 *AUB Condition*.

Before we describe the logic of the algorithm, we first introduce two notations:

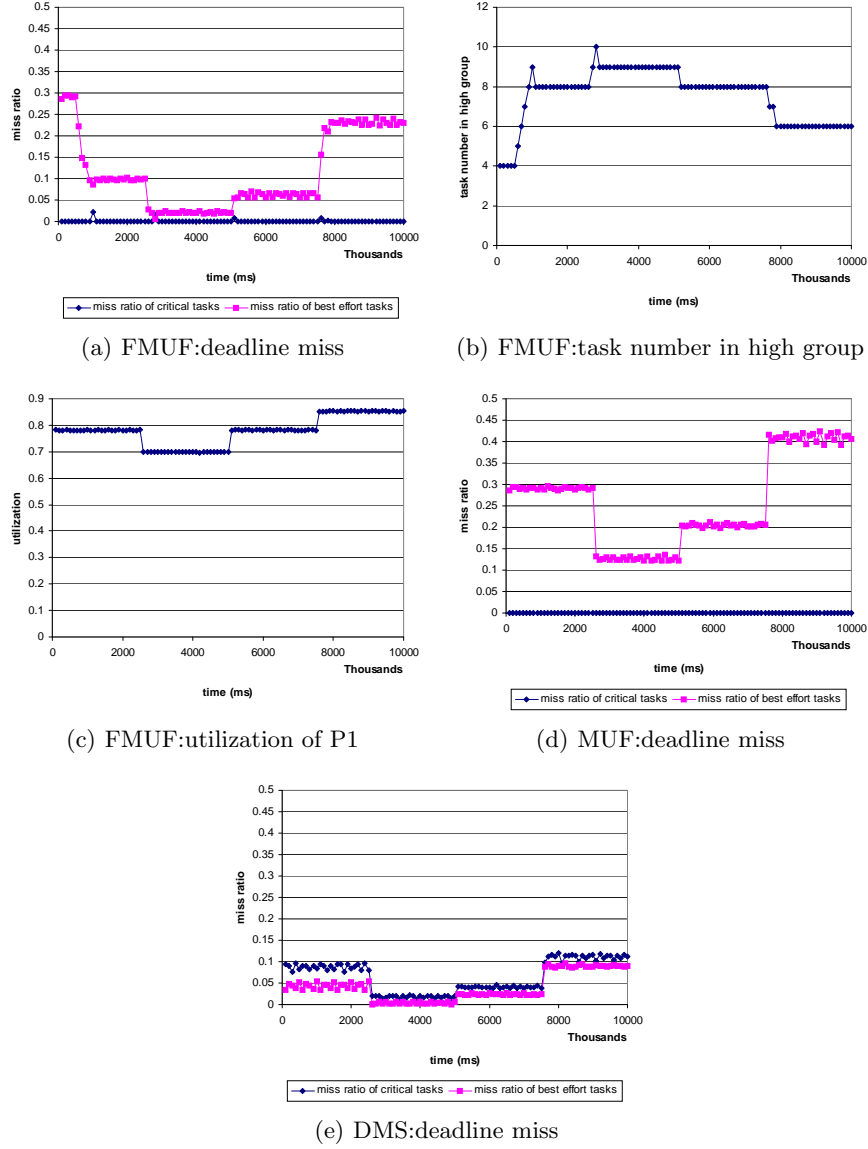
- $B_h$ : set of *best effort* tasks in the *high* group
- $B_l$ : set of *best effort* tasks in the *low* group

#### The Logic of FMUF

1. At the start time of the system, place all *mission-critical* tasks into the *high* group (by assigning high priority to them), and add all *best effort* tasks into the *low* group (by assigning low priority to them);
2. in the end of every sampling period, check the AUB condition
  - (a) **If** AUB condition is satisfied: select one task  $T$  from  $B_l$  and check the new AUB condition for the *high* group after including  $T$ ; if new AUB condition is not violated, move  $T$  into the *high* group; select another task from  $B_l$  and repeat this test until all tasks in  $B_l$  have been tested
  - (b) **Else** AUB condition is violated: move one task  $T'$  from  $B_h$  to the *low* group and check the new AUB condition for the *high* group after excluding  $T'$ ; if new AUB condition is not satisfied yet, select another task from  $B_h$  and repeat this process until the new AUB condition is satisfied or  $B_h$  is empty

### 3 Simulation Results

In this section, we evaluate the performance of the first approach presented in Section 2.2. The simulation runs on the EUCON simulator with a medium-sized workload that comprises of 11 end-to-end tasks. The task set includes 4 mission-critical tasks and 7 best-effort ones. Each task has 6 subtasks, which are deployed on 6 different processors (for simplicity, subtask  $i$  on processor  $i$ ,  $1 \leq i \leq 6$ ). The workload parameters are shown in Table 1. ET1-ET6 are corresponding to the execution times of subtask1-subtask6. There are only 6 different execution times: 35,40,55,65,70, and 90. Criticality = 1 means mission-critical task; criticality = 0 is corresponding to best-effort task. The time unit of execution time and period is millisecond. We assume each task's end-to-end deadline is equal to its period. In the beginning, only first 10 tasks run. Task 11 will arrive later. The control period  $T_s = 100s$ . Other two parameters for FMUF are chosen like this:  $N = 5$ , threshold = 5%.



**Fig. 1.** Experimental results: FMUF, MUF, and DMS

In the experiment, the system runs for 10000 seconds. We create three scenarios to evaluation the performance of FMUF: 1) at 2500 seconds, execution times of all subtasks are decreased by 10%; 2) at 5000 seconds, task 11 arrives; 3) at 7500 seconds, execution times of all subtasks are increased by 10%. In order to evaluate the performance of FMUF, we compare it with two baselines: MUF and DMS. We plot the results in Figure 1. The FMUF control operation is trig-

**Table 1.** workload parameters(ms)

Tasks	ET1	ET2	ET3	ET4	ET5	ET6	period	criticality
1	55	40	65	55	40	65	700	1
2	90	65	70	90	65	70	1000	1
3	65	70	65	70	55	65	900	1
4	35	40	40	35	35	40	500	0
5	70	65	65	55	65	70	800	0
6	70	65	90	70	90	70	1200	0
7	40	55	35	40	40	35	600	0
8	65	55	55	70	40	55	700	0
9	70	65	65	90	70	65	900	0
10	35	40	35	35	40	35	400	0
11	65	55	65	70	65	70	700	1

gered four times: in the initial stage, three best-effort tasks are moved into high group; after scenario 1, two more best-effort tasks are moved into high group; after scenario 2, two best-effort tasks are move back to low group; after scenario 3, another two best-effort tasks are degraded into low group. The results shows that FMUF can provide performance isolation for mission-critical tasks.

## References

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2. Tarek F. Abdelzaher, Gautam H. Thaker, Patrick J. Lardieri, I.: A Feasible Region for Meeting Aperiodic End-to-End Deadlines in Resource Pipelines. ICDCS (2004) 436-445