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Distributed Channel Allocation Algorithms for Wireless Sensor Networks

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Distributed Channel Allocation Algorithms for Wireless Sensor Networks

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Abstract—Interference between concurrent transmissions can cause severe performance degradation in wireless sensor networks (WSNs). While multiple channels available in WSN technology such as IEEE 802.15.4 can be exploited to mitigate interference, channel allocation can have a significant impact on the performance of multi-channel communication. This paper proposes a set of distributed algorithms for near-optimal channel allocation in WSNs with theoretical bounds. We first consider the problem of minimizing the number of channels needed to remove interference in a WSN, and propose both receiver-based and link-based distributed channel allocation protocols. Then, for WSNs with an insufficient number of channels, we formulate a fair channel allocation problem whose objective is to minimize the maximum interference (MinMax) experienced by any transmission link in the network. We prove that MinMax channel allocation is NP-hard, and propose a distributed link-based MinMax channel allocation protocol. Finally, we propose a distributed protocol for link scheduling based on MinMax channel allocation that creates a conflict-free schedule for transmissions. The proposed decentralized protocols are efficient, scalable, and adaptive to channel condition and network dynamics. Simulations based on real topologies and data traces collected from a WSN testbed consisting of 74 TelosB motes have shown that our channel allocation protocols significantly outperform a state-of-the-art channel allocation protocol.

I. INTRODUCTION

Multi-channel communication is attractive to wireless sensor networks (WSNs) as an effective approach to reducing interference and enhancing spatial reuse. Channel allocation significantly influences the performance of multi-channel WSNs. It is particularly important in WSNs employing TDMA protocols where interfering transmissions scheduled at the same time slot must be assigned different channels. It is, therefore, important to allocate the channels to reduce interference and increase the number of concurrent transmissions.

In this paper, we formulate optimal channel allocation as constrained optimization problems, and propose a set of near-optimal distributed channel allocation protocols with theoretical bounds for WSNs. We first consider the problems of minimizing the number of channels needed to remove interference in a WSN for both receiver-based and link-based channel allocation. In a *receiver-based* channel allocation, each node is assigned a channel that it uses for receiving packets from any sender, while in a *link-based* channel allocation, every link is assigned a channel to be used for any transmission along that link. A receiver-based channel allocation is suitable for both CSMA/CA and TDMA protocols. A link-based channel allocation allows better spatial reuse due to the flexibility in

assigning different channels to different senders, but it is more suitable for TDMA protocols under which the receiver can switch to channels according to the expected sender scheduled in each time slot. Interference-free minimum channel allocation is NP-hard for both receiver-based (proven in [1]) and link-based (proven in this paper) allocation. We present near-optimal distributed protocols for both receiver-based and link-based channel allocation.

WSNs usually have a moderate number of channels (e.g., 16 channels specified IEEE 802.15.4), and noisy environments may further reduce the number of available channels due to blacklisting [2]. Therefore, there may not exist enough channels to remove all interference. Existing works on channel allocation with an insufficient number of channels usually consider receiver-based allocation and propose simple centralized heuristics [1], [3], [4]. A recently proposed distributed protocol for channel allocation in WSNs has addressed receiver-based allocation to minimize total interference suffered by all receivers [5]. In contrast, we formulate a link-based fair channel allocation problem whose objective is to minimize the maximum interference (MinMax) experienced by any transmission link in a WSN with an insufficient number of channels. The key advantage of the MinMax objective is that it can mitigate bottlenecks in a WSN where a node or link experiences excessive interference. We prove that MinMax channel allocation is NP-hard, and propose a distributed MinMax channel allocation protocol.

Since channel allocation cannot always resolve all transmission conflicts due to an insufficient number of channels, it is complemented by a time slot assignment algorithm to create a conflict-free schedule. We propose a distributed protocol for link scheduling based on MinMax channel allocation. The proposed algorithms are efficient, scalable, and adaptive to channel condition and network dynamics. We provide the time complexity and performance bound of each algorithm. Simulations using real topologies and data traces collected from a WSN testbed of 74 TelosB motes have shown that our channel allocation protocols significantly outperform a state-of-the-art protocol.

In the rest of this paper, Section II reviews related work. Section III describes the network model. Section IV formulates the problems. Sections V and VI present the proof of NP-hardness and the distributed protocols for interference-free and MinMax channel allocation, respectively. Section VII presents the link scheduling protocol. Section VIII presents evaluation results. Section IX concludes the paper.

II. RELATED WORKS

Multi-channel MAC protocol has been widely studied for ad-hoc networks [6]–[16]. However, these protocols are not suitable for WSNs for various reasons. First, the protocols in [8], [12]–[16] assume that the hardware is able to listen to multiple channels simultaneously. But each sensor device is usually equipped with a single radio transceiver (e.g., TelosB mote equipped with IEEE 802.15.4 Chipcon CC2420 radio) that cannot transmit and receive at the same time, and cannot operate on different channels simultaneously. Second, the protocols in [6], [7], [10], [11] use RTS/CTS for channel negotiation. But, due to limited bandwidth in WSNs, the MAC layer packet size in WSNs is much smaller (typically 30~50 bytes) than that of general ad hoc networks (typically 512+ bytes). Hence, RTS/CTS control packets constitute significant overhead for WSNs. Third, the protocol in [9] involves a centralized solution through LP relaxation of the underlying mixed integer linear program. But sensor devices are characterized by low memory and limited processing capacity making them unsuitable for such heavy-weight computations.

MMSN [17] is the first multi-channel protocol proposed for WSN. MMSN ignores routing information for channel allocation. In contrast, we propose routing-aware channel allocation protocols that do not assign channels to the links not involved in traffic. Tree-based Multi-Channel Protocol (TMCP) proposed in [18] uses the distance-based interference model which does not hold in practice as shown by recent empirical studies [4]. TMCP has been extended in [4] to employ inter-channel RSS models for interference assessment in channel allocation [4]. All these protocols are *centralized*, and lack any approximation bound. The protocols proposed in [19]–[22] use simple heuristics for channel hopping based on channel condition. These protocols do not address interference-free minimum channel allocation or minimizing the maximum interference, which are the focus of our work.

The interference-aware channel allocation algorithm in [3] assigns a channel to each flow in a WSN. In [1], receiver-based interference-free minimum channel allocation has been proven to be NP-hard. It also shows that minimizing schedule length for multi-channel arbitrary network is NP-hard, and presents a constant factor approximation algorithm for unit disk graph [1]. The above algorithms [1], [3] are *centralized*. In contrast, we provide *distributed* protocols for interference-free channel allocation, fair channel allocation, and link scheduling. Due to frequent topology changes and network dynamics, distributed protocols are more suitable for WSNs.

The state-of-the-art distributed protocol proposed in [5] for channel allocation in WSN addresses receiver-based allocation. It adopts a game theoretic approach to minimize total interference suffered by all receivers. In contrast, we address a link-based fair channel allocation protocol that minimizes the maximum interference (MinMax) experienced by any transmission link across the network. The key advantage of the MinMax objective is that it can mitigate bottlenecks in a WSN where a node or link experiences excessive interference.

In addition, we propose interference-free minimum channel allocation as well as distributed algorithm for link scheduling based on MinMax channel allocation.

III. NETWORK MODEL

A WSN consists of a set of sensor nodes. A node, called the *base station*, serves as the sink of the network. A *communication link* $e = (u, v)$ indicates that the packets transmitted by node u may be received by v . We assume that every communications link is symmetric. This assumption holds for WSNs relying on acknowledgement for reliable communication (e.g., WirelessHART networks [2] based on IEEE 802.15.4). An *interference link* $e = (u, v)$ indicates that u 's transmission interferes with any transmission intended for v even though u 's transmission may not be successfully received by v . Thus, any two concurrent transmissions that happen on the same channel are *conflicting* if there is an interference link from one's sender to the other's receiver. Several practical protocols [23], [24] exist that model interference in WSNs using Signal-to-Noise plus Interference Ratio (SNIR). In such models, a set of transmissions on the same channel is conflict-free if the SNIR of all receivers exceeds a threshold. For example, RID [25] is a distributed protocol for determining interference links in a WSN based on Received Signal Strength (RSS) measurements.

We model a WSN as an *Interference-Communication* (IC) graph, a notion introduced in [26]. In the IC graph $G = (V, E)$, V is the set of sensor nodes (including the sink s); E is the set of communication or interference links between the nodes. A subset of the communication links forms the routing tree that is used for data collection at the sink. Let $E_T \subseteq E$ denote the set of links in the routing tree. Any link $e = (u, v)$ in E_T indicates that v is the parent of u . For any node u , we use p_u to denote its parent in the routing tree. Since the transmissions along non-tree links do not aim at the receiver, every non-tree link is an *interference link*. $E_I = E - E_T$ is the set of all interfering links in the IC graph. Any link $e = (u, v)$ in E_I indicates an interference link from u to v . A node cannot both send and receive at the same time, nor can it receive from more than one sender at the same time. The set of channels available in the WSN is denoted by M . We use m to denote $|M|$ i.e. the total number of channels. Without loss of generality, we assume that the channels are numbered through 1 to m .

IV. PROBLEM FORMULATION

In *receiver-based channel allocation*, each sensor node is assigned a fixed channel to receive message; the neighbors which have messages to deliver to it should use this channel to send. In this allocation, the leaves (i.e., nodes without children) in the routing tree do not receive any message, and hence are not assigned any channel. Let the nodes that receive message (i.e., the nodes other than leaves) be denoted by $R \subset V$. Therefore, the *receiver-based channel allocation* is a function $f : R \mapsto M$, where M is the set of channels.

In *link-based channel allocation*, every link $e \in E_T$ is assigned a channel so that every transmission along that link happens on that channel. In contrast to receiver-based channel

allocation, here for the same receiver, different senders can use different channels, thereby reducing more interferences. Any *link-based assignment* is a function $f : E_T \mapsto M$. Since every node has unique sending link, a link-based channel assignment function can also be defined as $f : V - \{s\} \mapsto M$, where s is the root (i.e., the sink) of the routing tree and it does not send to anyone. Thus every sender in the network is assigned a channel. For reception, the receiver uses the same channel that the sender uses to transmit.

Note that the interference caused by siblings (in the routing tree) to each other cannot be resolved by channel assignment. This can be resolved through a time-slot assignment. Therefore, for channel allocation purpose, we are concerned only about interference through non-tree links E_I , and simply use the term ‘conflict’ to denote the interference through these links. In the worst-case, the maximum number of transmissions that can be conflicting through interference links with a transmission along link (u, v) is equal to the sum of incoming interference links of v and outgoing interference links of u . Thus, we define *conflict of transmission link (u, v)* or *conflict of node u* as the maximum number of transmissions that can be conflicting through interference links with a transmission of node u . For a node u , in a channel assignment f , we use $C(u, f)$ to denote its conflict, and define as follows:

$$C(u, f) = |\{z | ((z, p_u) \in E_I \vee (u, p_z) \in E_I) \wedge f(z) = f(u)\}|$$

That is, $C(u, f)$ counts the total number of nodes that use the same channel as u 's and that has either an outgoing interfering link to the parent of u or an incoming interfering link to its parent from u . The higher the value of $C(u, f)$, the more the transmission of u has chances of conflict.

Problem 1: Receiver-based interference-free channel allocation. The number of non-overlapping channels is usually fixed and limited in practice. Our first objective is to minimize the total number of channels to remove all interferences in the IC graph $G = (V, E)$. Let $f(R)$ denote the range of function $f : R \mapsto M$, i.e., the set of channels used in f . In *receiver-based interference-free channel allocation*, our objective is to determine a channel assignment $f : R \mapsto M$ so as to

$$\begin{aligned} \text{Minimize} \quad & |f(R)| \\ \text{subject to} \quad & C(u, f) = 0, \forall (u, v) \in E_T \end{aligned}$$

Problem 2: Link-based Interference-free channel allocation. While receiver-based channel allocation is simple in the sense that a receiver can avoid switching to different channels for different senders, it can end up with extra interference for some transmission link, thereby limiting the communication possibilities for some nodes. Such a limitation of receiver-based channel allocation can be significantly overcome by adopting link-based allocation (discussed in Section V). In *link-based interference-free channel allocation*, our objective is to determine a channel assignment $f : V - \{s\} \mapsto M$ to

$$\begin{aligned} \text{Minimize} \quad & |f(V - \{s\})| \\ \text{subject to} \quad & C(u, f) = 0, \forall u \in V - \{s\} \end{aligned}$$

Problem 3: Minimizing Maximum interference (MinMax) channel allocation. The number of channels required to remove all interference may be greater than the total available channels. Therefore, when the available channels are not sufficient to remove all interference, a fair channel allocation is the one that minimizes the maximum interference experienced by any transmission link in G . Since link-based channel allocation allows better spatial reuse of channels, we use link-based allocation for MinMax objective. In MinMax channel allocation, our objective is to determine a link-based channel assignment $f : V - \{s\} \mapsto M$ so as to

$$\begin{aligned} \text{Minimize} \quad & \max\{C(u, f) | u \in V - \{s\}\} \\ \text{subject to} \quad & f(u) \in M, \forall u \in V - \{s\} \end{aligned}$$

Problem 4: Link scheduling. After MinMax channel allocation, a conflict-free schedule is required to avoid transmission conflicts through both tree (transmission) links and the residual interference links. This needs to be resolved through time slot assignment. To simplify the optimization problem for conflict resolution, we solve the problem in two different stages. That is, after channel allocation in Stage 1, we consider the link scheduling in Stage 2. In TDMA, a transmission needs one time slot, and a sequence of time slots forms a *frame*. The frame is repeated continuously. Every link is assigned a relative time slot within a frame and it is activated at that slot of the frame. Therefore, here our objective is to schedule all links to minimize the frame length. Thus, for link scheduling, after MinMax channel allocation, our objective is to determine a time slot assignment $g : E_T \mapsto \{1, 2, 3, \dots\}$ so as to

$$\text{Minimize} \quad |g(E_T)|$$

V. INTERFERENCE-FREE CHANNEL ALLOCATION

A. Receiver-based Channel Allocation

We first consider receiver-based channel allocation to minimize the number of channels to eliminate all interference. This problem has been proven to be NP-hard in [1]. In the following, we provide a distributed algorithm based on *vertex-coloring* for this problem.

Two receivers are called *interfering* if the transmission of some child of one receiver is interfered by the transmission of some child of the other receiver. In order to eliminate all interference, every receiver must be assigned a channel that is different from all of its interfering receivers' channels. Therefore, for the given IC graph $G = (V, E)$, we can assume a *receiver-based conflict-graph*, denoted by $G_R = (R, E_R)$, that consists of all receivers R as nodes, and an edge (in E_R) between every interfering receiver pair. For example, Figure 1(b) shows the receiver-based conflict-graph of the IC graph of Figure 1(a). In an IC graph, we use dotted lines and solid lines to indicate interference links and transmission links, respectively. Considering every *channel* as a *color*, vertex-coloring of G_R provides the solution for receiver-based interference-free channel allocation in G to minimize the number of channels (colors).

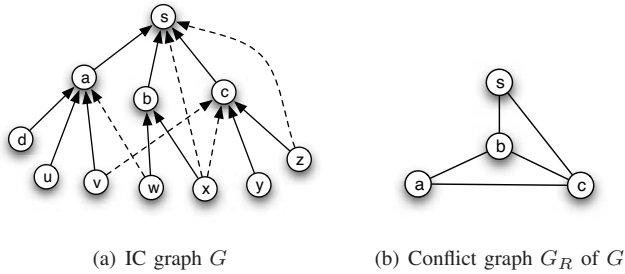


Fig. 1. IC graph and receiver-based conflict graph

For vertex-coloring in distributed manner, the best known deterministic algorithm [27] employs $D^{1+O(1)}$ colors, where D is the maximum degree of the given graph. The distributed methods for vertex-coloring available in the literature of theoretical computer science [27] involve multiple phases. A phase starts only after its previous phase converges. Since the WSN devices are characterized by low power and resources, these algorithms are too heavy-weight for WSNs. Here we present a simple and deterministic distributed protocol suitable for WSNs, which can employ at most $\Delta_R + 1$ channels, with Δ_R being the degree of the receiver-based conflict graph.

Let $N_R(u)$ denote the neighbors of node u in G_R . In our distributed method, every node $u \in R$ has to communicate with its neighbors $N_R(u)$ in G_R . Note that two neighbors u and v in G_R may not be one-hop away from one another in IC graph G . In such cases, u and v communicate with one another by increasing their transmission power like what is done in [25], [26]. If this is not possible, communication between u and v is done through the end-to-end route between u and v . Channel allocation is done iteratively and every round consists of communication between the neighbors in G_R . In every communication round, all nodes use the same channel. Once the algorithm converges, every node uses the channel determined by the algorithm for subsequent communication. The distributed receiver-based interference-free channel allocation protocol consists of the following steps comprising a procedure that is invoked iteratively:

- 1) In the beginning, every node $u \in R$ is assigned channel 1 (the smallest numbered channel). In every round, each node $u \in R$ broadcasts a message containing its ID and chosen channel to its neighbors $N_R(u)$.
- 2) Considering the current channel allocation among neighbors $N_R(u)$, every node u repeatedly switches to the smallest channel not used by any of its neighbors. Two neighbors cannot switch channels simultaneously. If two neighbors in G_R want to switch at the same time, the node with the smallest ID wins (as a local agreement among neighbors) and switches channel.
- 3) After choosing the channel, each node u broadcasts its chosen channel in a message (that also contains its ID) to its neighbors $N_R(u)$ in G_R .
- 4) The procedure is repeated until every node has chosen a channel different from its neighbors in G_R and cannot choose a channel that is smaller than its current channel.

The above algorithm converges when every node in G_R has

chosen a channel different from those of its neighbors $N_R(u)$, and cannot switch to a smaller channel. In every round, the total number of messages that are sent or received by a node u is $O(|N_R(u)|)$. Theorem 1 proves the convergence of the algorithm. Theorem 2 shows that the algorithm requires at most $\Delta + 1$ channels, where Δ is the maximum degree of G .

Theorem 1: Receiver-based interference-free channel allocation algorithm converges in $|E_I|$ rounds, where $|E_I|$ is the total number of interfering links in G .

Proof: Until the algorithm converges, in every round at least one node switches its channel that is different from its neighbors in the receiver-based conflict graph G_R . If a node u switches to a channel that is different from its neighbors' channels, the interference links between u and its neighbors $N_R(u)$ are removed. Since no two neighbors in G_R switch channels in the same round, at least one interfering link in G is removed in every round. Since the total interfering links in G is $|E_I|$, the algorithm converges in at most $|E_I|$ rounds. ■

Theorem 2: Receiver-based interference-free channel allocation algorithm requires at most $\Delta + 1$ channels, where Δ is the maximum degree in G .

Proof: Let Δ_R be the maximum degree of G_R . The channels are numbered 1,2,3, ... in increasing order. Every node initially has channel 1. Every time a node switches channel, it switches to the smallest channel not used by the neighbors. Hence, the largest possible channel to which a node can switch is $\Delta_R + 1$, which happens if all first Δ_R channels are chosen by its neighbors in G_R . Therefore, the algorithm employs at most $\Delta_R + 1$ channels. Since $\Delta \geq \Delta_R$, the theorem follows. ■

The above algorithm is adaptive to network dynamics. If the routing tree is reconstructed due to any node or link failure, the algorithm will be invoked. It will run quickly and converge.

B. Link-based Channel Allocation

Receiver-based allocation can end up with extra interference for some transmission link, thereby limiting the communication possibilities for some nodes. As a result, when all transmission conflicts are completely resolved through a time slot assignment phase, the schedule length becomes longer if a receiver-based allocation is adopted. This limitation can be significantly overcome by adopting a link-based allocation since it allows better spatial reuse. This is illustrated in Figure 2 through a simple example considering $m=2$. The number in the rectangle beside every receiver shows its assigned channel. Under this receiver-based allocation, every time node w transmits, none of a 's children should transmit. This problem can be avoided using a link-based channel allocation instead (as shown beside the links) by assigning channel 1 to node w , and channel 2 to node x .

A reduction similar to the one used in [1] (that proves that receiver-based interference-free channel assignment is NP-hard) can also be used to prove that link-based interference-free channel allocation is NP-hard as shown in Theorem 3.

Theorem 3: Given a routing tree T on an IC graph $G = (V, E)$, and a total of m channels, it is NP-complete to decide

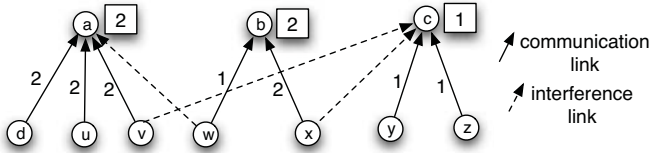


Fig. 2. Link-based channel allocation

whether there exists some channel allocation f to the links in T such that G becomes interference-free.

Proof: The problem is in NP since, given an instance of the problem, we can verify in $O(|E|)$ time whether the network is interference-free. Following reduction from vertex-coloring implies NP-hardness. Given any instance $\langle \mathbb{G}, k \rangle$ of the vertex-coloring problem in graph $\mathbb{G} = (\mathbb{V}, \mathbb{E})$, we create a sink node s as the parent of every $u \in \mathbb{V}$, and create a child for every u . Now for every edge $(u, v) \in \mathbb{E}$, we create an interfering link between u 's child and v (or between v 's child and u). This constructs an IC graph $G = (V, E)$. A channel allocation f uses the color of $u \in \mathbb{V}$ as the channel of u 's child, and uses any channel c , $1 \leq c \leq k$, for u in G . Thus, \mathbb{G} can be vertex-colored with k colors if and only if f can remove all interference links from G using k channels. ■

Now we present a distributed algorithm for link-based channel allocation to minimize the number of channels in order to eliminate all interfering links. This approach is also similar to the distributed vertex-coloring adopted for receiver-based allocation in the previous subsection.

Two senders in G are called *interfering* if one's transmission is interfered by the other. In order to eliminate all interference, every sender's transmission link must be assigned a channel that is different from those of its interfering senders. Therefore, for the IC graph $G = (V, E)$, we can assume a *link-based conflict-graph*, denoted by $G_L = (V - \{s\}, E_L)$, that consists of all senders $V - \{s\}$ as nodes, and an edge (in E_L) between every interfering sender pair. For example, Figure 3 shows the link-based conflict-graph of the IC graph of Figure 1(a). Considering every *channel* as a *color*, vertex-coloring of G_L provides the solution for link-based interference-free channel allocation in G to minimize the number of channels (colors).

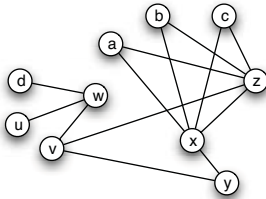


Fig. 3. Link-based conflict graph G_L of G

Using the same distributed algorithm as the one used for receiver-based channel allocation in the preceding subsection, we now vertex color graph G_L . When the algorithm converges, every sender (i.e., every sender's transmission link) is assigned a channel that is different from any interfering sender's channel. This algorithm converges within $|E_T|$ rounds, and employs at most $\Delta_L + 1$ channels, where Δ_L is the maximum degree in G_L (proofs are similar to those of Theorems 1 and 2).

VI. DISTRIBUTED MINMAX CHANNEL ALLOCATION

Note that WSNs usually have a moderate number of channels (e.g., 16 channels for WSNs based on IEEE 802.15.4), and noisy environments may further reduce the number of available channels due to blacklisting [2]. Therefore, there may not exist enough channels to remove all interference using the algorithms presented in the previous section. In such a situation, we adopt MinMax channel allocation whose objective is to minimize the maximum interference experienced by any transmission link across the network. Since receiver-based allocation may not minimize the maximum interference experienced by a transmission link (Subsection V-B), we follow a link-based approach for MinMax channel allocation.

We first prove that MinMax allocation is NP-hard by showing that its decision version is NP-complete (Theorem 4).

Theorem 4: Given a routing tree T on an IC graph $G = (V, E)$, m channels, and an integer k , it is NP-complete to decide if there exists a channel allocation f to the links in T such that the maximum conflict in G is at most k .

Proof: When $k = 0$, the decision problem of the theorem represents a decision version of the link-based interference-free channel allocation (Problem 2) that has been proved to be NP-complete in Theorem 3. Therefore, this decision problem is a generalization of the decision version of Problem 2 and, hence, is NP-complete. ■

Now we present a distributed algorithm for MinMax channel allocation. In the protocol, every node needs to communicate with its neighbors in link-based conflict graph G_L (see Subsection V-B and Figure 3 for G_L) to compute its conflict. For any node u , the set of its neighbors in G_L is denoted by $N_L(u)$. Communication in the neighborhood in G_L is done based on the same approach presented in the previous section. Distributed MinMax channel allocation algorithm consists of the following procedure that is invoked iteratively:

- 1) Before the invocation of the procedure, every node $u \in V - \{s\}$ is assigned a random channel in the range between 1 and m . Every node $u \in V - \{s\}$ broadcasts a message containing its ID and assigned channel to its neighbors $N_L(u)$ in G_L .
- 2) Considering the current channel allocation among the neighbors in G_L , every node calculates its conflict $C(u, f)$ and broadcasts again to the neighbors $N_L(u)$.
- 3) For each node u , once it receives the message containing $C(v, f)$ from each neighbor v in G_L , node u calculates its conflict $C(u, f)$ on every channel. Any channel used by a neighbor v with $C(v, f) > C(u, f)$ is considered unavailable at u . That is, node u excludes all channels used by the neighbors with higher conflicts in the current round. This is done because switching to such a channel increases the neighbor's conflict which may increase the maximum conflict in the network. Among the available channels, node u switches to the channel that results in the smallest $C(u, f)$, breaking ties arbitrarily. Two neighbors cannot switch channels simultaneously. If two neighbors want to switch at the same time, the node with

the smallest ID wins and switches its channel.

- 4) After choosing the channel, every node broadcasts its chosen channel to its neighbors in G_L .
- 5) The procedure is repeated as long as some node u can decrease its $C(u, f)$ using its available channels.

In each communication round, all nodes use the same channel for communication. Once the algorithm converges, every node uses the channel determined by the algorithm for subsequent communication. Each node u needs to send or receive $O(|N_L(u)|)$ messages in a round. The algorithm converges when no node can decrease its conflict using its available channels. Theorem 5 proves its convergence.

Theorem 5: MinMax Channel Allocation converges in $|E_I|$ rounds, where $|E_I|$ is the total interfering links in G .

Proof: Since MinMax algorithm is repeated as long as some node u can decrease its $C(u, f)$ using its available channels, in every round at least one node switches its channel. Assuming the neighbors of u in G_L keep their channels unchanged, changing the channel of u that decreases $C(u, f)$ implies that the total number of interference links between u and its neighbors decreases. Since no two neighbors in G_L switch channel simultaneously, at least one interfering link in G is removed in every round. Hence, similar to Theorem 1, the algorithm converges in at most $|E_I|$ rounds. ■

Theorem 6: After MinMax Channel Allocation converges, the maximum conflict in G is at most $\lfloor \frac{C_{\max}}{m} \rfloor$, where C_{\max} is the maximum conflict in G under single channel.

Proof: Let $d(u)$ denote the degree of node u in link-based conflict graph G_L of G . The value $d(u)$ is equal to the conflict of u under single channel. We first prove that, when MinMax Algorithm converges, at most $\lfloor \frac{d(u)}{m} \rfloor$ neighbors in G_L can have the same channel as the one assigned to u , for any node u . Suppose to the contrary, after the algorithm converges, there exists some node v such that $\lfloor \frac{d(v)}{m} \rfloor + 1$ neighbors in G_L have the same channel as the one assigned to v . Let c be the channel assigned to v , and $Z \subseteq N_L(v)$ be the neighbors of v in G_L that have been assigned channel c . Now according to *the pigeon-hole principle*, there must be at least one channel $c' \neq c$ such that at most $\lfloor \frac{d(v)}{m} \rfloor - 1$ neighbors of v have been assigned channel c' . If $\exists z \in Z$ such that $C(v, f) \leq C(z, f)$, then z will switch to channel c' since it can decrease its $C(z, f)$. If $C(z, f) \leq C(v, f)$, then v will switch to channel c' since it can decrease its $C(v, f)$. Both cases contradict with the hypothesis that the algorithm has converged. Therefore, when MinMax Algorithm converges, at most $\lfloor \frac{d(u)}{m} \rfloor$ neighbors in G_L can have the same channel as the one assigned to u , for any node u . Since C_{\max} is equal to the maximum degree in G_L , the theorem follows. ■

The key advantage of the MinMax objective is that it can mitigate bottlenecks in a WSN where a node or link experiences excessive interference. The simulation results (presented in Section VIII) indicate that the MinMax objective is more effective than minimizing the total interference in the network in terms of critical network metrics such as latency.

Adapting to channel condition and network dynamics. Since

MinMax Algorithm is decentralized, it can easily adapt to channel condition and network dynamics. In the algorithm, every node switches to a channel among its available channels. For simplicity, our presentation has assumed that all nodes have the same set of available channels in the beginning. Due to variability of external interference patterns on different channels and on different parts of the network, a channel that is very good to some node may be very noisy for some other nodes. That is, the list of available channels may be different for different nodes. This can be easily handled in MinMax Algorithm. The noisy channels at a node can be blacklisted and considered *unavailable* to that node. A node will be allowed to switch only to some available (good) channel. Similarly, whenever a new channel degrades or the condition of a noisy channel improves, the algorithm is simply invoked, run, and quickly converged. Similarly, if the routing tree is reconstructed due to any node or link failure, the algorithm will be invoked. It will run quickly and converge.

VII. DISTRIBUTED LINK SCHEDULING

Note that channel allocation cannot resolve all transmission conflicts in a WSN due to two reasons. First, the number of available channels is limited and may not suffice to remove all interference. Second, each WSN device is equipped with a half-duplex radio that prevents a node from both transmitting and receiving at the same time, and also prevents reception from two senders simultaneously. Therefore, a channel allocation is complemented by a time slot assignment. Namely, any two conflicting transmissions are assigned different time slots. While this can be achieved through a joint channel allocation and time slot assignment, performing channel allocation and time slot assignment in two different phases simplifies this optimization problem. In this section, we present a distributed algorithm for time slot assignment after MinMax channel allocation. Namely, we first perform MinMax channel allocation. Then, in the second phase, we perform a time slot assignment that avoids transmission conflicts through both tree links and the residual interference links to create a conflict-free schedule.

In the time slot assignment algorithm, every link is assigned a relative time slot in a frame, and the link is activated at that slot of the frame. The frame is repeated continuously. Note that, after MinMax channel allocation, the network can still be considered as a new IC graph with reduced interference. Therefore, a proof similar to Theorem 3 implies that scheduling all links to minimize the frame length is NP-hard. We provide a distributed method for time slot assignment that minimizes the frame length.

To resolve the conflict through both tree links and residual interference links after MinMax channel allocation, we determine a schedule conflict graph G_S of IC graph G as follows:

- Ignore all interfering links that are removed by MinMax channel allocation.
- Add links between siblings. The links between parent and children remain unchanged.
- For every interfering link (u, v) from u to v that still exists after MinMax channel allocation f , add a link from

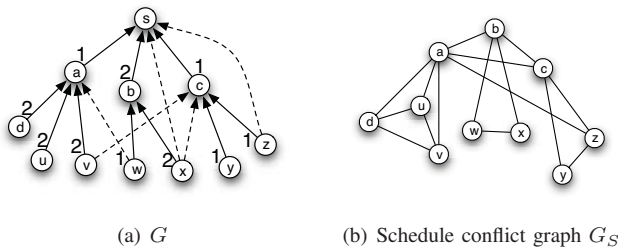


Fig. 4. IC graph and schedule conflict graph

u to every child z of v with $f(z) = f(u)$.

For the IC graph G shown in Figure 1(a), let Figure 4(a) shows the channel allocation, where the number beside a sender shows its assigned channel. Then Figure 4(b) shows its schedule conflict graph G_S . In a TDMA schedule, any two nodes that are neighbors in G_S must be scheduled on different time slots. We use the same distributed algorithm as the one used for interference-free channel allocation. We run the algorithm considering schedule conflict graph G_S . Now, instead of channel, we allocate a time slot to every node in G_S . Every node starts with slot 1. In each round, the nodes switch to the smallest slot not assigned to any neighbor in G_S . The maximum time slot assigned to a node indicates the length of the frame, since the frame will repeat after this slot.

Theorem 7: The frame length determined by the distributed link scheduling algorithm is at most $\lfloor \frac{C_{\max}}{m} \rfloor + \Delta_T + 1$, where C_{\max} is the maximum conflict in G under single channel, Δ_T is the maximum degree of the routing tree.

Proof: According to Theorem 2, the total time slots used in the frame is at most $\Delta_S + 1$, where Δ_S is the maximum degree in G_S . After MinMax channel allocation, $\Delta_S \leq \lfloor \frac{C_{\max}}{m} \rfloor + \Delta_T$. Hence, the bound follows. ■

VIII. EVALUATION

We evaluate our channel allocation and link scheduling protocols on the topologies of an indoor WSN testbed [28] spread over two buildings (Bryan Hall and Jolley Hall) of Washington University in St. Louis. The testbed consists of 74 TelosB nodes each equipped with a Chipcon CC2420 radio compliant with IEEE 802.15.4. We have developed a discrete-event simulator that operates based on interference data traces collected from the testbed. The traces were obtained by having each node in the testbed take turns broadcasting a sequence of 50 packets. All nodes operated on channel 26 of IEEE 802.15.4. While the application transmits packets as soon as possible, the MAC layer applied for each transmission a randomized back-off uniformly distributed in the interval [10ms, 170ms]. The batch of 50 packets takes 4.5s on average to transmit. The remainder of the nodes recorded the Received Signal Strength (RSS) of the packets they receive. The short delay between the transmissions of packet pertaining to the same batch allows us to capture the short-term variability of RSS. We have collected 7 sets of data traces at 7 transmission (Tx) power levels: -15 , -10 , -7 , -5 , -3 , -1 , 0 dBm. Collecting the data traces over three consecutive days captured the long-term variability. RSS traces collected from the 74-node testbed are used to

configure the simulations. Figure 5 shows the interference and communication edges on the testbed when every node's Tx power is set to -5 dBm. The topology shown in Figure 5 is embedded on the floor plan of two buildings.

The network topologies used in the simulations are based on RSS traces collected from the testbed. We determine the communication and interference links between nodes as follows. A node A may communicate with a node B if node B 's RSS average during A 's transmissions exceeds a threshold of -85 dBm. Prior empirical studies have shown that links with RSS above this threshold typically have high packet reception rate (PRR) [29]. Interference links are determined based on RID protocol [25]. RID models interference as a graph that is constructed as follows. To determine whether the transmissions of other nodes can interfere with a communication link (A, B) , RID calculates the Signal to Noise Plus Interference Ratio (SNIR) at node B for each set of k senders ($k = 3$ in our setup) assuming they transmit simultaneously as A transmits to B . For each set of senders $S(B)$, RID computes the SNIR at B when A and the set of senders $S(B)$ transmit simultaneously. The RSS of a link is computed as the average of the four 50 packet batches collected from the testbed. The RSS of missing packets is overestimated to equal the receiver sensibility of CC2420 (-90 dBm). If the computed SNIR is below a threshold a link from each node in $S(B)$ to B is added as an interference link. The SNIR threshold was set to 5 dB consistent with empirical studies that showed that meeting this threshold is usually sufficient for correctly decoding packets in the presence of interference [4], [25]. The routing tree on a topology is constructed based on high quality links.

For a wider range and scalability of tests, we also evaluate our protocols on randomly generated networks. A random network is generated with an edge-density of 50%, i.e. with $n(n-1)50/200$ edges for a network with n nodes. PRR along each link is assigned randomly in a range $[0.60, 1.0]$. A node with the highest degree is selected as the sink. A subset of links with $\text{PRR} \geq 0.90$ forms the routing tree. All other links are considered as interference links.

A. Distributed Interference-free Channel Allocation

We first evaluate our algorithms for interference-free minimum channel allocation. We evaluate them in terms of *required number of channels* and *convergence time*. The first metric has been compared with its theoretical bound, and that required by a well-known centralized heuristic, called *Largest Degree First* (LDF) [1] (where a node is assigned the first available frequency in non-increasing order of degrees).

Figure 6 shows the number of channels and rounds (to converge) of 1 run for our interference-free channel allocation on testbed topologies at different Tx power. For receiver-based channel allocation (Figure 6(a)), our protocol requires no more than 6 channels (marked as 'Dis Receiver-based' in the figure) in every topology, and these values are less than the theoretical upper bound. While LDF is inherently more effective at the cost of centralized behavior, the figure indicates that the numbers of channels required by the centralized LDF



Fig. 5. Testbed topology at -5 dBm Tx power (solid green lines are communication link; dotted red lines are interference link; the sink is colored in blue)

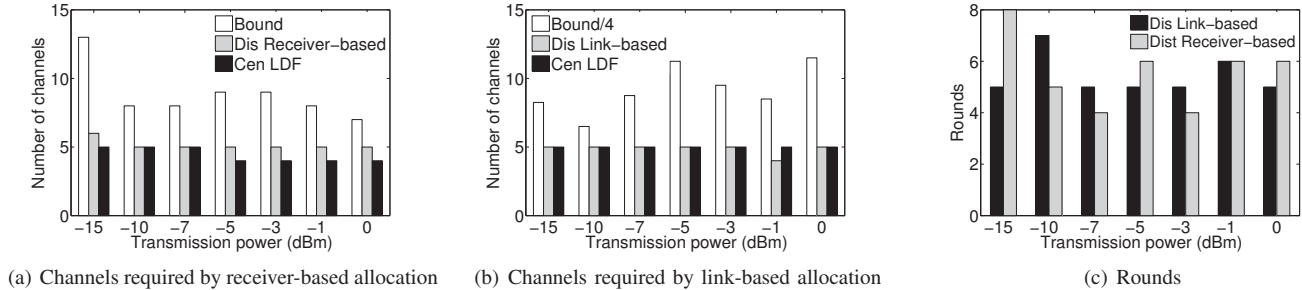


Fig. 6. Channel allocation on testbed topologies to remove all interferences

and that by our distributed protocol vary at most by 1. For the link-based allocation (Figure 6(b)), the number of channels required by our protocol is much less than its theoretical bound. The theoretical bound (one fourth of which is drawn in the figure) tends to be higher than receiver-based bound because the degree of the link-based conflict graph is naturally much larger than that of the receiver-based one. Here also the numbers of channels required by the centralized LDF are at most 1 less than those required by our distributed protocol. As shown in Figure 6(c), our both protocols converge in at most 7 rounds.

Figure 7 shows the results on random topologies with different number of nodes. For receiver-based channel allocation (Figure 7(a)), our protocol requires only 23 channels for a 700-node network. The figure indicates that the numbers of channels required by the centralized LDF and that by our distributed protocol vary at most by 1. For the link-based allocation (Figure 7(b)), the number of channels required by our protocol is 32 for a 700-node network. Here also the numbers of channels required by the centralized LDF are at most 1 less than those required by our distributed protocol. As shown in Figure 6(c), our both protocols converge in at most

31 rounds for a 700-node network. The results indicate that our interference-free distributed channel allocation protocols are highly effective both in terms of required number of channels, and in terms of time to converge.

B. Distributed MinMax Channel Allocation

Now we evaluate the MinMax algorithm. We plot the maximum conflict among all transmission links and the average conflict per transmission link after channel allocation. On every topology, each algorithm is run 5 times. Each data point is the average of 5 runs. Since there exists no protocol that minimizes the maximum interference, we compare the performance of our MinMax algorithm with that of GBCA [5], the only known distributed protocol that minimizes the total interferences in the network in a receiver-based allocation. We also compare the performance with a *centralized greedy approach* that works as follows. Every time the greedy algorithm determines the link that experiences the maximum conflict. If there exists a link such that switching its channel to a different one decreases the maximum conflict (without increasing another link's interference beyond the current maximum), then it switches to that channel. Any sender that does not affect

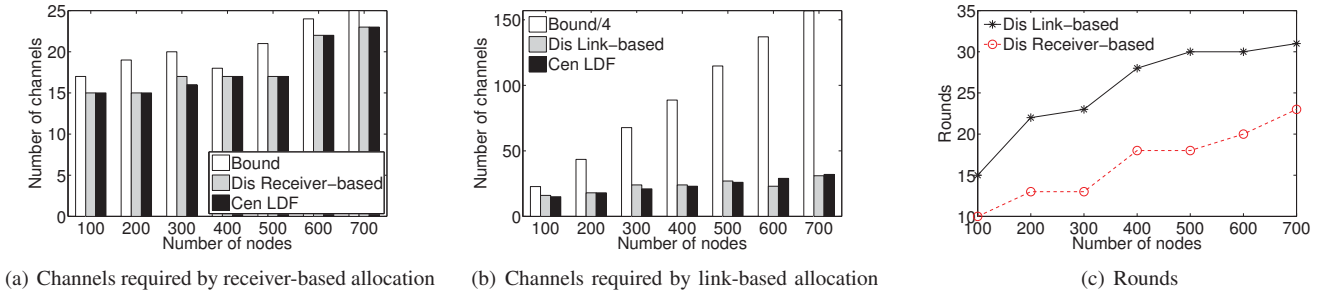


Fig. 7. Channel allocation on random topologies to remove all interferences

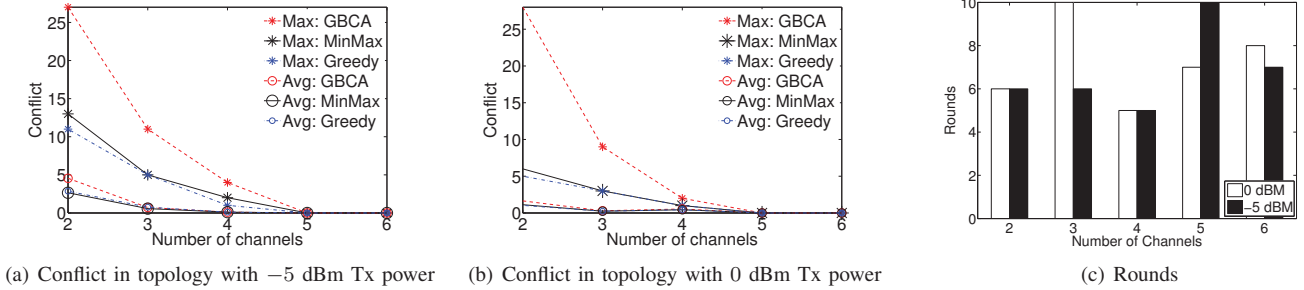


Fig. 8. MinMax channel allocation on testbed topologies

the maximum conflict switches to the channel that results in maximum decrease in its own conflict.

Figure 8 shows the performance of MinMax protocol on testbed topologies under varying number of channels. For the topology at -5 dBm Tx power, Figure 8(a) shows that the maximum conflict in GBCA using 2 channels is 27 while that in MinMax is only 13. The average conflict per link is 4.55 in GBCA, and 2.87 in MinMax. The centralized greedy heuristic results in a maximum conflict of 11, and an average of 2.85 per link. For the topology at 0 dBm Tx power, Figure 8(b) shows that the maximum conflict in GBCA using 2 channels is 28 while that in MinMax is only 6. Here also the centralized greedy is only a little better than our distributed MinMax allocation. Both maximum and average conflict in GBCA are higher than those in MinMax allocation since GBCA does not aim to minimize the maximum conflict (suffered by a transmission link) across the network. Since the testbed consists of only 74 nodes, we cannot see any performance gap when the number of channels is increased beyond 5. In fact, neither MinMax nor GBCA does require more than 5 channels. Figure 8(c) shows that the MinMax protocol converges in no more than 10 rounds for every topology.

Figure 9 shows the performance of MinMax protocol on random topologies with different number of nodes. Figure 9(a) shows that the performance gap between GBCA and MinMax increases with the increase of network size. In a 700-node network with 2 channels, the maximum conflicts in GBCA, MinMax, and centralized greedy heuristic are 470, 246, and 240, respectively; the average conflicts per link in GBCA, MinMax, and centralized greedy heuristic are 183, 123, and 120, respectively. Figures 9(b) and 9(c) shows the similar

results using 4 and 8 channels, respectively. The results show that MinMax protocol is highly effective in minimizing the maximum interference. It also results in less (compared to GBCA) average conflict which is very close to that of the centralized greedy algorithm. Figure 9(d) shows that the MinMax protocol converges very quickly (within 47 rounds) when the number of nodes is no greater than 300. For a 700-node network with 4 channels, it converges in 98 rounds.

C. Network Performance Under MinMax Channel Allocation

Here we implement our distributed link scheduling protocol after both MinMax and GBCA channel allocation. We consider TDMA with each time slot of 10ms (similar to WirelessHART [2] based on 802.15.4). For scheduling, every node periodically generates a packet in every 0.5s resulting in a flow to the sink. We record the maximum packet delay and the average packet delay in both protocols. The delay of a packet is counted as the difference between the time when it is delivered to the sink and the time when it was released at its source. In every run, a set of source nodes is selected randomly. Each data point is the average of 5 runs.

Figure 10 shows the delays under different number of flows on the testbed topology at -5 dBm Tx power. Figure 10(a) shows that the maximum delay among 70 flows under GBCA using 2 channels is 40.65s while that under MinMax allocation is only 34.40s. The average delay per packet is 8.60s under GBCA, and 7.24s under MinMax. Figures 10(b) and 10(c) shows the results for 3 and 4 channels, respectively. In every setup, the 95% confidence interval remains within $\pm 1.7s$ for maximum delay, and within $\pm 0.43s$ for average delay for each protocol. The performance difference between GBCA

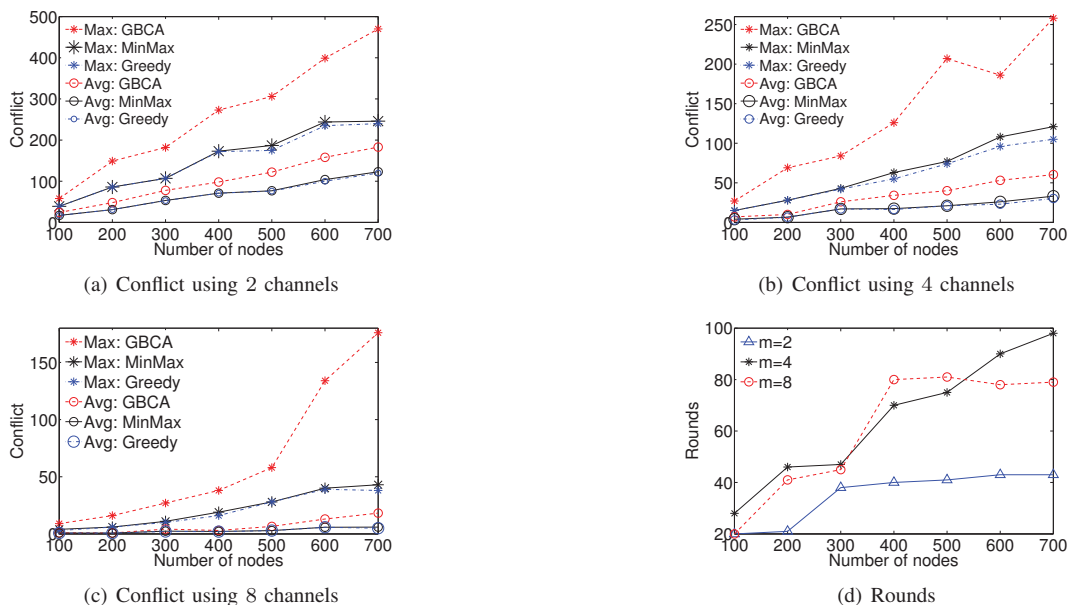


Fig. 9. MinMax channel allocation on random topologies

and MinMax is more pronounced in larger networks as shown for random topologies of 400 (excluding the sink) nodes in Figure 11. For 400 flows and 2 channels (Figure 11(a)), the maximum delay is 692.61s under GBCA, and 526.68s under MinMax; the average delay per packet is 155.18s under GBCA, and 117.04s under MinMax. For 400 flows and 4 channels (Figure 11(b)), the maximum delay is 607.49s under GBCA, and 473.49s under MinMax; the average delay is 140.03s under GBCA, and 105.08s under MinMax. For 400 flows and 8 channels (Figure 11(c)), the maximum delay is 478.81s under GBCA, and 451.00s under MinMax; the average delay is 106.29s under GBCA, and 80.02s under MinMax. In every setup, the 95% confidence interval remains within $\pm 16.7s$ for maximum delay, and within $\pm 4.65s$ for average delay for each protocol. The results indicate that our MinMax channel allocation is more effective in terms of packet latency.

IX. CONCLUSION

We have proposed a set of distributed algorithms for near-optimal channel allocation in WSNs. We have presented both receiver-based and link-based channel allocation for minimizing the number of channels to remove interference in a WSN. For WSNs with an insufficient number of channels, we have proposed a link-based fair channel allocation protocol that minimizes the maximum interference (MinMax) experienced by any transmission link in the network. The key advantage of the MinMax objective is that it can mitigate bottlenecks in a WSN where a node or link experiences excessive interference. We have also proposed a distributed link scheduling protocol based on MinMax channel allocation. Simulations using both random topologies and real topologies and data traces collected from a WSN testbed of 74 TelosB motes have shown

that our channel allocation protocols significantly outperform a state-of-the-art protocol.

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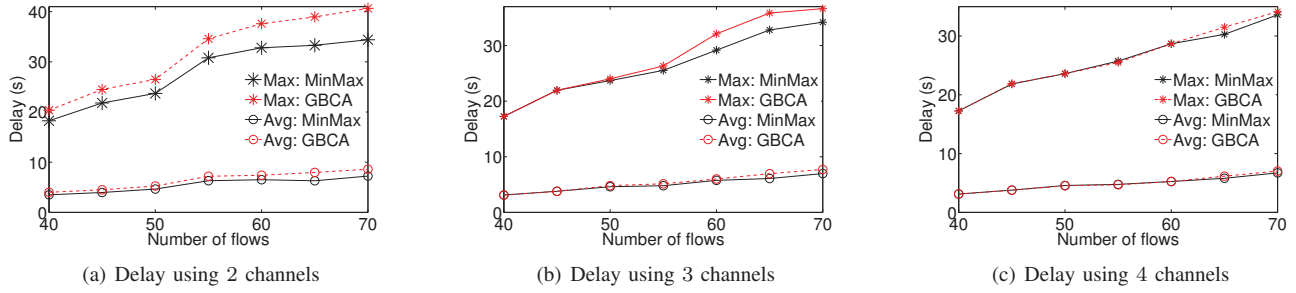


Fig. 10. Network performance on testbed topology at -5 dBm

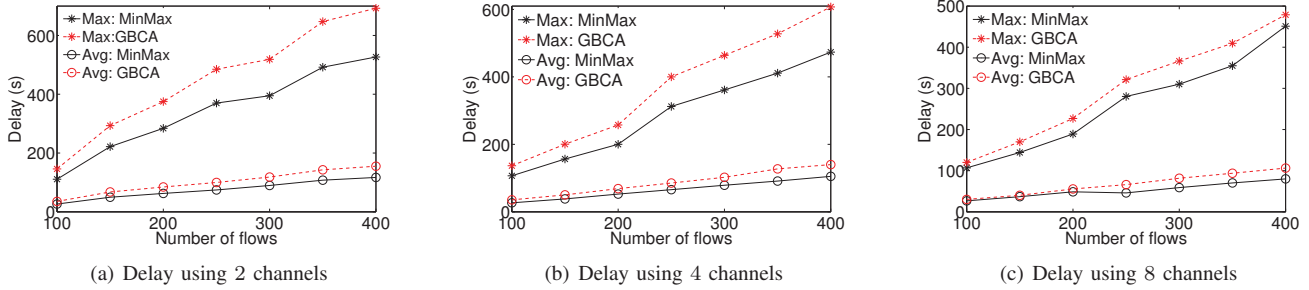


Fig. 11. Network performance on random topology of 400 sensor nodes

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