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# Human Trajectory Prediction in the Interaction between Human and Unmanned Vehicles

#### Introduction

In the realm of shared spaces where humans and robots coexist, safeguarding interactions is vital. This study presents a data-driven trajectory prediction method that enhances robot action planning by integrating human danger awareness, promoting both safety and operational efficiency in human-robot environments.

#### **Problem Formulation**

#### **Robot Model**

- State and Action: The Robot's state and action at time t are represented by  $x_R(t) \in \mathbb{R}^{n_R}$  and  $u_R(t) \in U_R \subset \mathbb{R}^{m_R}$ .
- **Dynamics:** The robot's dynamics are modeled by:

$$x_R(t+1) = f_R(x_R(t), u_R(t))$$

This updates the robot's state based on its current state and action.

• **Objective Function:** The objective function, denoted as  $Q_B^g$ , incorporates the Euclidean distance from the robot's current state to its goal state and the action cost:

$$Q_R^g(x_R(t), u_R(t), g_R) = \theta_1 \|x_R(t) - g_R\|^2 + \theta_2 \|u_R(t)\|^2$$

where  $\theta_1$  and  $\theta_2$  are weighting parameters.

• Optimization Problem: The robot solves the following optimization problem over the prediction horizon  $T_R$ :

$$u_{R}^{*}(t:t+T_{R}-1) = \begin{cases} \arg\min & \sum_{k=t}^{t+T_{R}-1} Q_{R}^{g}(\cdot) \\ \text{s.t.} & u_{R}(k) \in U_{R} \quad \forall k, \\ & Model(1) \\ & P_{\mathsf{Coll}}(k) \leq P_{\mathsf{th}} \quad \forall k \end{cases}$$

where  $k = t+1, \ldots, t+T_R, u_R^*(t:t+T_R-1) = [u_R^*(t) \ldots u_R^*(t+T_R-1)]^+$ ,  $P_{Coll}(k) \in [0,1]$  is the probability of a collision between the human and robot at prediction time instant k, and  $P_{th} \in [0, 1]$  is a threshold value.

### Human Model

- State and Action: The Human's state and action at time t are represented by  $x_H(t) \in \mathbb{R}^{n_H}$  and  $u_H(t) \in U_H \subset \mathbb{R}^{m_H}$ .
- Dynamics: The human's dynamics are modeled by:

$$x_H(t+1) = f_H(x_H(t), u_H(t))$$

This updates the human's state based on its current state and action.

 Objective Function: The human's objective function is a weighted sum of two components-the goal-reaching and the safety objectives:

$$Q_H^g(x_H(t), u_H(t), g_H) = \theta_3 \|x_H(t) - g_H\|^2 + \theta_4 \|u_H(t)\|^2$$

$$Q_H^s(x_H(t), u_H(t), x_R(t)) = \theta_5 e^{-\theta_6 \|x_H(t) - x_R(t)\|^2}$$

where  $\theta_3, \theta_4, \theta_5$ , and  $\theta_6$  are weighting parameters.

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- (1)

- (2)

- (3)

- (4)
- (5)
- (6)

 Action Selection: The human selects the action that optimizes the combination of the goal and safety objectives:

 $u_H^*(t) = \arg\min_{u_H \in U_H} \left(\eta_1 Q_H^g(\cdot) + \beta \eta_2 Q_H^s(\cdot)\right)$ 

where  $\eta_1, \eta_2 \in R_{>0}$  are the weighting factors and  $\beta \in \{0, 1\}$  represents the human's danger awareness.

# **Trajectory Prediction**

#### **Model Structure**



Fig. 1. Recurrent Neural Network (RNN) model for trajectory prediction

#### Inputs:

- Robot's Past Positions:  $p_R^{t-T_O:t}$ , from time  $t T_O$  to current time t.
- Human's Past Positions:  $p_H^{t-T_O:t}$ , from time  $t T_O$  to current time t.
- Danger Awareness Coefficient:  $\beta$ , indicating the human's perception of potential risks.

#### • Outputs:

- A sequence of predicted future positions of the human over the prediction horizon, denoted by  $p_H^{1:TR}$ .
- Main Modules of the Danger-Informed Model:
  - Robot State Encoder: An LSTM module that processes the sequence of past robot positions and encodes it into a state representation,  $z_R$ .
  - Human State Encoder: An LSTM module that processes the sequence of past human positions and encodes it into a state representation,  $z_H$ . This module also incorporates the estimated value of the danger awareness coefficient,  $\beta$ .
  - Decoder Module: An LSTM module that takes the concatenated state representations of the robot and human,  $z_R$  and  $z_H$ , and predicts the future trajectory of the human.

# Experiments & Results

# **Experiment Setup and Data Generation**

- Simulation Environment: A two-dimensional space where both the human and robot navigate towards dynamically updating goal positions.
- Past and Future Data: Positions and velocities of the human and robot are recorded over  $N_{sim}$  time steps. For each time step t, the dataset includes past observations over a horizon of  $T_O$  and future positions over a horizon of  $T_H$ .





Fig 2. Human Robot Interaction sample trajectories.

#### **Prediction Results**

- Feed the trajectory data into the prediction model.
- Generate the human trajectory prediction.
- Compare with the ground truth human future position to evaluate the performance of the prediction model.



Fig 3. Sample output of the prediction system.

### Conclusion

This research advances the predictive modeling of human trajectories with a datadriven approach that accounts for human danger awareness. The resulting model demonstrates potential for enhancing robot decision-making, fostering safer and more efficient human-robot interactions. Future integration into action planning schemes promises significant improvements in the cohabitation of humans and autonomous systems in shared environments.

#### References

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